

Robust Mapping of Process Networks to Many-Core Systems using Bio-Inspired Design Centering

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ABSTRACT

Embedded systems are often designed as complex architectures with numerous processing elements. Effectively programming such systems requires parallel programming models, e.g. task-based or dataflow-based models. With these types of models, the mapping of the abstract application model to the existing hardware architecture plays a decisive role and is usually optimized to achieve an ideal resource footprint or a near-minimal execution time. However, when mapping several independent programs to the same platform, resource conflicts can arise. This can be circumvented by remapping some of the tasks of an application, which in turn affect its timing behavior, possibly leading to constraint violations. In this work we present a novel method to compute mappings that are robust against local task remapping. The underlying method is based on the bio-inspired design centering algorithm of L_p -Adaptation. We evaluate this with several benchmarks on different platforms and show that mappings obtained with our algorithm are indeed robust. In all experiments, our robust mappings tolerated significantly more run-time perturbations without violating constraints than mappings devised with optimization heuristics.

KEYWORDS

dataflow programming, design centering, KPN, SDF, MAPS, L_p -Adaptation

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1 INTRODUCTION

Multi- and manycore architectures have permeated the majority of today's embedded systems. Examples include ARM big.LITTLE systems [17], the Qualcomm Snapdragon family of processors [31],

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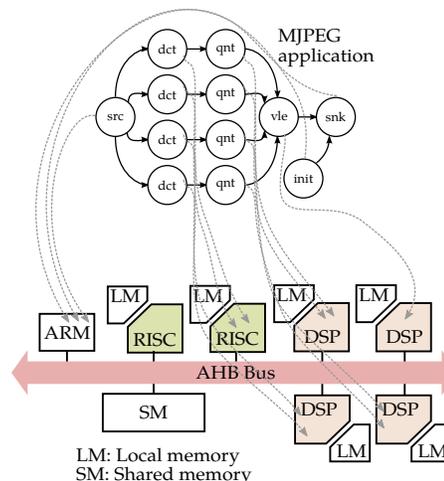


Figure 1: The mapping problem.

Texas Instruments Keystone [3] or the He-P2012 platform [8]. The quick spread of parallel architectures took tool providers by surprise and software development became a major concern.

Several programming models have been proposed in academia to solve the parallel programming problem. Popular examples in the embedded domain are dataflow-based or task-based programming models, particularly well-suited for streaming and multimedia applications. These models have in common that applications are represented as a graph of interacting entities (i.e., graph nodes) that communicate over statically defined channels (i.e., graph edges)¹. In dataflow graphs or process networks, the entities cannot communicate over shared memory, which makes these models appropriate for distributed memory architectures. Many languages and models exist to represent such graphs, e.g., Cal [13], YAPI [11], C for process networks [38] or the Distributed Object Layer (DOL) [45].

With applications represented as graphs, programmers face the *mapping problem*, i.e., which hardware resources should be used to run computation and to implement communication (see Figure 1). The mapping problem has been thoroughly studied in the embedded domain, e.g., for performance and soft real-time [4, 6, 14, 21, 24, 29], for energy efficiency [25] or for reliability [10] (see also overviews in [26, 41]). Most of the approaches seek to find a near-optimal *static* mapping for a single application and compile-time, mostly for ensuring time predictability. Authors have also looked into

¹In task-based programming models edges represent dependencies.

the problem of dealing with multiple applications competing for resources. Scenarios have been used to characterize the way application may interact [34]. Spatial isolation in which applications are given *shapes* of the hardware has also been proposed to provide time-predictability in the presence of multiple applications [48].

Most of previous work has focused on computing a fixed mapping, which is enforced by a runtime manager or by strict spatial isolation. The underlying assumption is that nothing unpredictable may modify the mapping decisions at runtime. This can be achieved in bare metal implementations, but is less probable in higher-end embedded systems that run a full fledged mainstream operating system and run unpredictable workloads. In this paper, we look at how to compute mappings that not only meet real-time constraints but are robust to slight variations at runtime, e.g., by re-mapping decisions from the operating system. To find a robust mapping, one must not only find a near-optimal solution using an optimization process, but also has to characterize the “volume” of feasible solutions around that one solution. Intuitively speaking, the larger the volume, the more robust the solution is. To determine robust mappings we apply *design centering*, a technique known for the design of feasible circuits given parameter variations in individual components [16]. In particular, we use a recent bio-inspired algorithm that is well-suited for non-convex feasibility spaces. Additionally, it returns a quality measure based on the estimated volume along with the design center [2, 27].

As main contribution, this paper analyzes for the first time design centering algorithms for the mapping problem. In particular, we study the applicability of design centering approaches to compute mappings that are robust to local re-mapping decisions. We introduce algorithmic modifications to make design centering applicable to the characteristics of the design space of mapping problems. We analyze benchmark applications from the streaming and multimedia domains on two different multicores with different characteristics, using a state-of-the-art mapping flow for applications represented as Kahn Process Networks (KPNs). We report promising results that demonstrate the higher robustness of the mapping computed with design centering. More specifically, we show that robust mappings for most applications tolerate 70% to 98% of the variations, as opposed to an average of $\approx 50\%$ for mappings computed with standard heuristics. We believe these results open more possibilities to adapt the problem to compute mappings that are robust to other types of variations, most notably, input-dependent execution characteristics. Even though we used KPNs as programming model, the approach is applicable to other similar programming models as well.

The rest of this papers is organized as follows. Section 2 provides background on design centering algorithms and introduces the programming flow used in this paper, whereas Section 3 provides the specific of the L_p adaptation algorithm we used. Then, Section 4 describes how we applied design centering to the mapping problem. The method is evaluated in Section 5 and related approaches are treated in Section 6. Finally, we draw conclusions and discuss future work in Section 7.

2 BACKGROUND

As mentioned above, in this paper we apply design centering to the mapping problem (cf. Figure 1). Before explaining the proposed

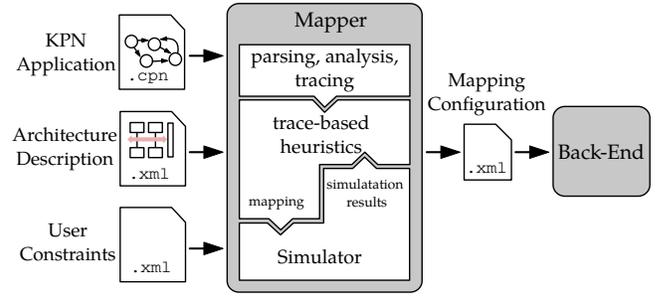


Figure 2: Overview of the mapping flow.

approach, this section provides details about the mapping problem, as well as the concrete tool flow used and a brief introduction to design centering approaches.

2.1 KPN mapping flow

Out of many mapping frameworks, we use the parallel flow of the MAPS framework [5], now commercially available in the SLX Tool Suite from Silexica [39]. This state-of-the-art, to which we will refer as *mapper* in the following, includes a fast internal simulator for a variety of multicore platforms. Having a fast simulator is key for applying design centering as will be discussed in Section 4. Additionally, the mapper supports an expressive parallel programming model, based on KPNs, that allows to represent more applications compared to static dataflow models, like Synchronous Data Flow. An overview of the programming flow is shown in Figure 2. The major components are discussed in the following.

The mapper receives a KPN application written in the language “C for process Networks” [38]. In a KPN graph, nodes are computational processes that exchange data only through FIFO channels (the edges of the graph) using atomic data items called tokens. Processes may have an arbitrary control flow, holding internal state, and accessing input and output channels in a data-dependent fashion (i.e., not statically analyzable at compile time). Extra inputs to the mapper are an abstract model of the target platform and user-defined constraints. The latter includes real-time and resource constraints, among others. The model of the target platform contains a specification of the processing elements, the interconnect and the memory architecture (including latencies and communication bandwidths).

The mapper uses execution traces from profiling runs to capture the runtime behavior of the processes. Based on the traces, several heuristics are available to compute a mapping [6]. The mapping includes an assignment of processes to processors, a scheduling policy for processes running on the same processor, a mapping of logical communication channels to physical resources, and sizes for all buffers. Broadly speaking, heuristics would iterate to improve the mapping and to try and meet the user constraints. To evaluate the quality of a mapping and whether the mapping is feasible, the mapper uses an internal discrete event simulator. The simulator fetches cost models from the architecture description and replays the traces according to the suggested mapping, taking runtime overheads into account. It returns a Gantt chart of the execution,

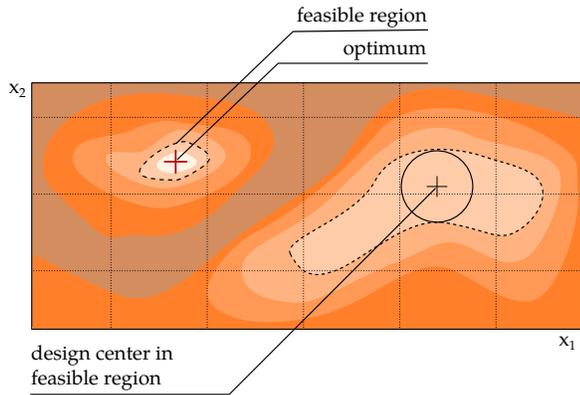


Figure 3: Illustration of design centering.

buffer utilization statistics, and an estimated energy consumption, among others.

Once a feasible mapping has been found, the mapper exports it in a so-called mapping configuration. This descriptor is then passed to the back-end, which generates code accordingly.

2.2 Design Centering

Design centering is a long-standing and central problem in systems engineering. It is concerned with determining design parameters of a system that guarantee operation within given specifications and are robust against parameter variations. While *design optimization* aims to determine the design that *best* fulfills (one aspect of) the specifications, *design centering* wants to find the design that meets the specifications most *robustly*. Traditionally, this problem has been considered in electronic circuit engineering [16], where a typical task is to determine the nominal values of electronic components (e.g., resistances, capacitances, etc.) such that the circuit fulfills some specifications and is robust against manufacturing tolerances in the components. An illustration for a two-dimensional design space, i.e., with two parameters, is shown in Figure 3. The figure also contains the contour of a fictive cost function and two regions with sets of feasible solutions (marked with dashed lines). While optimization is concerned with finding the optimum (red cross in the figure), design centering would opt for the solution that allows more variation in the parameters without leaving the feasible set (the black cross in the figure).

There are usually many designs that fulfill the specifications. Each design is described by a number n of design parameters and can hence be interpreted as a vector in \mathbb{R}^n . The region (subspace) of the parameter space that contains the designs for which the system meets the specifications is called the *feasible region* $A \subset \mathbb{R}^n$ (see disjoint regions in Figure 3). Depending on available side-information about design specifications, different operational definitions of the *design center* $\mathbf{m} \in A$ exist, including the *nominal design center*, the *worst-case design center*, and the *process design center* [37]. Here, we follow the statistical definition of the design center [23] and seek among all parameter vectors $\mathbf{x} \in A$ the design center $\mathbf{m} \in A$ that represents the mean of a probability distribution $p(\mathbf{x})$ of maximal volume covering the feasible region A with a given *target hitting*

probability P . For convex feasible regions, using the uniform probability distribution over A and $P = 1$, the design center coincides with the geometric center of the feasible region (corresponding to the crosses in Figure 3).

One distinguishes between geometrical and statistical approaches to design centering. Geometrical approaches use simple bodies to approximate the feasible region, which is usually assumed to be convex [12, 35, 36]. Statistical approaches explore the feasible region by Monte-Carlo sampling. Since exhaustive sampling is not feasible in high dimensions, the key ingredient of statistical methods is a smart sampling proposal to find, and concentrate on, informative regions [42–44]. Most of the existing methods assume a convex feasible region, e.g., [36, 43], or differentiability of the specifications, e.g., [46]. Others require an explicit probabilistic model of the variations in the design parameters [35]. For the mapping problem dealt with in this paper, we cannot assume differentiability or convexity. Therefore, we use a recently proposed statistical method called L_p -Adaptation [2]. This method supports non-convex disconnected regions (like in Figure 3), and can handle arbitrary specification constraints as long as they can be decided for a given candidate design. In addition, the method also retrieves the radius and an estimated volume, providing an idea of how robust the design center is. The concrete algorithm is described in the next section.

3 ADAPTATION ALGORITHM

L_p -Adaptation [2] is an algorithm inspired by how robustness has evolved in biological networks, such as cell signaling networks, blood vasculature networks, and food chains [22]. It samples candidate designs from L_p -balls as proposal distributions, which are dynamically adapted based on the sampling history. Intuitively speaking, an L_p -ball is an n -dimensional ellipsoid according to a particular norm, the L_p norm. The dynamic affine adaptation of the L_p -balls is based on the concept of Gaussian Adaptation (GaA) [23], which continuously adapts the mean and the covariance matrix (describing correlations and scaling between the parameters) of a Gaussian proposal based on previous sampling success.

Combining the adaptation concept of GaA with the use of L_p -balls [37] as non-Gaussian proposals, L_p -Adaptation provides both efficient design centering and robust volume approximation. L_p -adaptation draws samples uniformly from an L_p -ball and iteratively adapts the mean and covariance matrix of an affine mapping applied to the balls. Importantly, the *target hitting probability* P , i.e., the probability of hitting the feasible region A with a sample is controlled as described below. The design center is then approximated by the mean of the final L_p -ball B , and the volume estimate is of the form $\text{vol}(A) \approx P \cdot \text{vol}(B)$, where $\text{vol}(B)$ is the volume of the current n -dimensional L_p -ball B . For improved sampling and adaptation efficiency, L_p -Adaptation uses an adaptive multi-sample strategy [18] that is considered state-of-the-art in bio-inspired optimization [19].

L_p -Adaptation can be interpreted as a synthetic evolutionary process that tries to maximize the robustness, rather than the fitness, of the underlying system. Robustness is measured in terms of the volume $\text{vol}(B)$ of an n -dimensional L_p -ball B , of which a certain fraction P (i.e., the target hitting probability) overlaps with the feasible region A . This ball is called an L_p -ball since it is part of the Banach space $L_p^n = (\mathbb{R}^n, \|\cdot\|_p)$. This basically means that we endow

the vector space \mathbb{R}^n with a norm different from the Euclidean one, namely $\|(x_1, \dots, x_n)\|_p = \sqrt[p]{|x_1|^p + \dots + |x_n|^p}$ for any $p \geq 1$.

Let us denote by $\mathcal{L}_p^n = \{B(\mathbf{m}, C) \mid \mathbf{m} \in L_p^n, C \in S_+^{n \times n}\}$ the set of all balls $B = B(\mathbf{m}, C) \subseteq L_p^n$ for a fixed n, p , where $\mathbf{m} \in L_p^n$ denotes the center of the ball, and $C \in S_+^{n \times n}$ is a symmetric positive-definite (covariance) matrix defining the linear map for scaling and rotation of the L_p -ball B , i.e.

$$B(\mathbf{m}, C) = \{C\mathbf{x} + \mathbf{m} \mid \mathbf{x} \in \mathbb{R}^n, \|\mathbf{x}\|_p \leq 1\}.$$

L_p -adaptation then seeks to maximize the following criterion:

$$\begin{aligned} & \max_{B=B(\mathbf{m}, C) \in \mathcal{L}_p^n} \text{vol}(B(\mathbf{m}, C)) & (1) \\ & \text{s.t.} & \mathbf{m} \in A. \\ & & \frac{\text{vol}(A \cap B(\mathbf{m}, C))}{\text{vol}(B(\mathbf{m}, C))} \geq P \end{aligned}$$

The hypervolume of an L_p -ball is completely determined by the volume of the unit L_p -ball (with zero mean and n -dimensional identity matrix $C = \mathbf{1}$) and the determinant of the matrix C . Thus, the robustness criterion can be rewritten as a non-convex log-det maximization problem:

$$\begin{aligned} & \max_{B=B(\mathbf{m}, C) \in \mathcal{L}_p^n} \log \det(C) & (2) \\ & \text{s.t.} & \mathbf{m} \in A. \\ & & \frac{\text{vol}(A \cap B(\mathbf{m}, C))}{\text{vol}(B(\mathbf{m}, C))} \geq P \end{aligned}$$

This objective function provides a natural non-convex extension of the maximum inscribed ellipsoid method [37]. For instance, if A is a convex polyhedron with known parameterization and $P = 1$, then Problem 2 is a convex problem that can be efficiently solved using interior point methods. However, in the general case, no efficient algorithms are known to solve Problem 2. L_p -adaptation approximately solves this problem by using a synthetic evolutionary process consisting of the four steps **Initialization**, **Sampling**, **Evaluation**, and **Adaptation**, which are repeated in iterations until a stopping criterion is fulfilled.

It is, however, important to properly control the target hitting probability P of L_p -Adaptation to the task at hand. The hitting probability must be neither too low, nor too high. Low hitting probabilities lead to low sampling efficiencies. High hitting probabilities lead to slower adaptation to the feasible region, which may prevent exploring remote parts of the feasible region. For a Gaussian proposal and a convex feasible region, a hitting probability of $\exp(-1)$ is information-theoretically optimal [23]. When sampling uniformly from L_p -balls over non-convex regions, no such result is available. We hence manually adapt the hitting probability depending on the task at hand, starting from $\exp(-1)$ as an initial value.

4 DESIGN CENTERING AND MAPPING

In this section we explain how we adapted the design centering (DC) algorithm to create robust mappings of KPN applications to many-core systems.

4.1 Integration into KPN Tool-Flow

In order to use the DC algorithm to create and evaluate mappings we have to integrate the DC algorithm into the KPN tool flow as

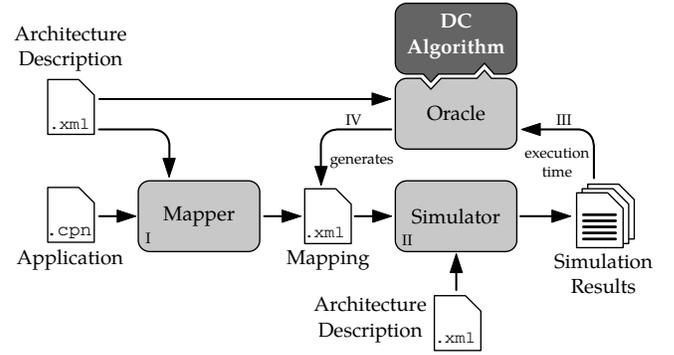


Figure 4: Integration of DC-Algorithm into SLX Tool Suite.

shown in Figure 4. For the integration, it is required to import mappings generated by the DC algorithm into the mapping flow. Similarly, the results of the discrete-event simulator of the mapping flow (recall Figure 2) must be interpreted by the oracle. That is, the function in the DC algorithm that decides, for a given point x in the design space, if the point x is feasible, i.e., if $x \in A$.

As first step (I), an initial mapping for a CPN application onto the target architecture is generated by the mapper. This is necessary since the starting point of the DC algorithm has to be member of the feasible set A . The initial mapping is then simulated (II) using a representative dataset as input. From the simulation results, it is possible to check for a variety of constraints. In this paper we restrict ourselves to checking for the total execution time, but the current constraint could be easily replaced by a more complex evaluation, e.g. the maximum execution time for different input data sets. Afterwards, the resulting execution time is fed to the oracle function (III) which triggers the DC algorithm to generate a new parameter set. In order to simulate the determined parameters, they must be interpreted as mapping and adapted to the given architecture (IV). This adaptation is carried out by the oracle function. The extracted parameter description includes the assignment of the cores to the respective processes only. This transfer of mapping-graphs to a parameter vector abstracts from the actual graphical structure and communication relations between cores. Thus, the DC algorithm has no knowledge about the underlying hardware architecture or communication structures. The newly generated mapping is simulated again to produce the next results (III) for the oracle function. The DC algorithm requires approximately 10,000-30,000 samples to obtain a valid DC. This does not mean every sample is a simulation, since many samples can refer to the same mapping. We implemented a cache that holds results of already simulated mappings for later use. This is important since the simulation time dominates the overall execution time of the algorithm.

4.2 Architectures

To apply the DC algorithm to the mapping problem, we need to leverage information about the target architectures themselves. In this paper, we use two architectures that provide sufficient processing elements for our evaluation. For our approach we used architectures with uniform processing elements, which simplifies the

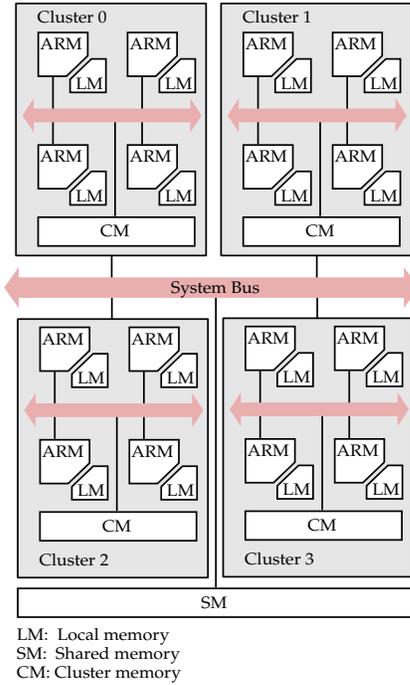


Figure 5: ARM SoC architecture

generation of mappings from the generated parameter set (cf. Section 4.1). It should be noted that there is no reason, in principle, why the tool flow should not work on heterogeneous architectures. It could be extended to target more heterogeneous architectures with moderate engineering effort.

- (1) A generic ARM SoC with a heterogeneous memory structure is used (cf. Figure 5). The chosen architecture contains 16 Cortex A9 cores with a clock frequency of 1GHz and a hierarchical bus system. Each core has a direct connection to a local L1 cache. In addition, 4 cores are grouped into one cluster sharing one L2 cache. In case that data has to be exchanged over boundaries of a cluster, a global main memory must be used. The latency of the required communication structures as well as the respective memory structures increase with decreasing locality. Thus, processes that are scheduled on the same core, provide the lowest communication latencies. The highest communication latency, on the other hand, comes from cores using the shared memory. However, mapping two processes to one core requires additional context switches each time the process is activated, which introduces additional latencies.
- (2) A homogeneous network on chip architecture as shown in Figure 6 consisting of 16 cortex A9 cores. In contrast to the previous architectures, there are no global memories available. The individual cores have local memories and are connected to a network on chip similar to the Epiphany III architecture from Adapteva [1]. The used simulation provides a system-level view of the NoC behavior without detailed simulation of routing contentions.

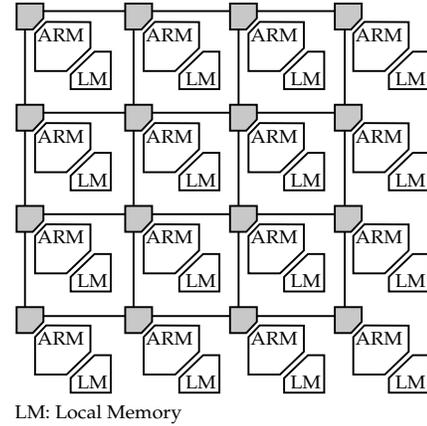


Figure 6: NoC Architecture

4.3 Mappings for Design Centering

In order to apply the L_p -Adaptation method, we need to encode mappings as vectors in the normed space L_p^n for some suitable n, p . To do this, we first have to understand precisely what a mapping is from a mathematical standpoint. Once we have done this, and have a (mathematical) set M of mappings, we can find a function $encode : M \rightarrow L_p^n$ for some suitable n, p . In order for this function $encode$ to have a valuable meaning, it should also capture an intuitive notion of *distance* between two mappings as the p norm in L_p^n . In other words, we have to find a mathematical description of mappings not only as a set M , but rather, as a metric space (M, d) , with a distance function d . We would then require some sort of compatibility: If $d(m_1, m_2)$ is small, we want $\|encode(m_1) - encode(m_2)\|$ to be small, in some sense. Ideally, we would like $encode$ to be an isometry (or an isometric embedding), i.e., $d(m_1, m_2) = \|encode(m_1) - encode(m_2)\|$ and bijective (injective). However, the discrete structure of mappings is ill-suited to find such a representation, and we should not expect to find a function $encode$ that is an isometry for any intuitive description of the mapping set M . On the other hand, we would ideally like $encode$ to be a bijective function (parametrization) of the set M , since we can then find exactly one point in the design space L_p^n for every mapping. Since M is finite and L_p^n uncountable, a bijective function will not exist. An injective function is imperative though, since otherwise we cannot uniquely determine a mapping from a point in the design-space L_p^n .

4.3.1 Encoding Mappings. Consider the example depicted in Figure 7A. In order to help the visualization, we coarsened the KPN of a two-channel audio filter to consist of only two processes with two channels: the source (*src*) and the sink (*snk*). The source process reads the filter file, splits both channels and performs an inverse Fast Fourier Transform (FFT) on each. Then, the sink channel filters each channel in the frequency domain and applies an FFT to convert back to the time domain. The figure shows three different mappings, each coded with a different color, onto Architecture 1 (Figure 5). Consider concretely the orange mapping, which maps the source to ARM₁₄ and the sink to ARM₁₅. Both FIFO channels are mapped to the shared L2 of Cluster 3, even though it is not explicitly shown

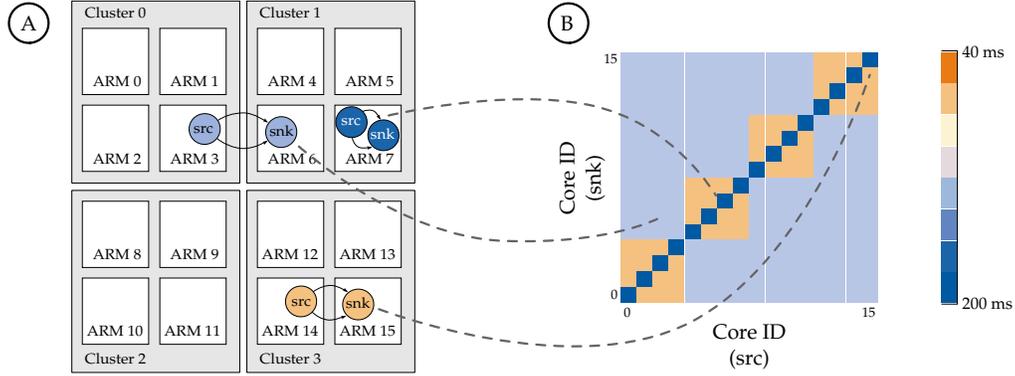


Figure 7: An example of a design space of mappings

in the figure. Such a KPN mapping is thus an assignment of KPN processes (and channels) to system resources. In this paper, we concentrate on process-to-core mappings. Mathematically, such an assignment is best described as a function. If we thus let K be the set of KPN processes, and R the set of system resources, then a KPN mapping is just a function $m : K \rightarrow R$. The orange mapping from Figure 7 A is, thus, the function

$$m : \{\text{src}, \text{snk}\} \rightarrow \{\text{ARM}_0, \dots, \text{ARM}_{15}\},$$

$$\text{src} \mapsto \text{ARM}_{14}, \text{snk} \mapsto \text{ARM}_{15} \quad (3)$$

Since the sets K and R are finite, we can describe the set R^K of such functions as the set of $|K|$ -tuples over R , $R^{|K|} = R^n$, if we set $n := |K|$. For this, we can fix an enumeration of K , $K = \{k_1, \dots, k_{|K|}\}$. We can thus encode the mapping m as:

$$\text{encode}(m) = (m(k_1), m(k_2), \dots, m(k_{|K|})) \in R^{|K|}$$

For the orange mapping in Figure 7A, the mapping of Equation 3, this would mean encoding it as the tuple $m \hat{=} (\text{ARM}_{14}, \text{ARM}_{15})$.

By fixating an enumeration of R in the same manner, this yields an embedding onto $\mathbb{R}^{|K|}$ as sets, i.e., encode is an injective function. The example above reduces to $m \hat{=} (14, 15)$ For the metric we first define a metric on the architecture, d_{arch} . This metric depends on the architecture itself, but is chosen such that $d_{\text{arch}}(\text{PE}_i, \text{PE}_i) = 0$ for all i , i.e. for all PEs. Furthermore, we chose the distance according to the latencies, such that $d_{\text{arch}}(\text{PE}_i, \text{PE}_j) < d_{\text{arch}}(\text{PE}_i, \text{PE}_k)$, if the latency between PE_i and PE_j is always smaller than that between PE_i and PE_k . For example, in the architecture depicted in Figure 7, we have

$$d_{\text{arch}}(\text{ARM}_i, \text{ARM}_j) = \begin{cases} 0 & \text{if } i = j \\ 1 & \text{for all } i, j \text{ if } i, j \text{ in the same cluster} \\ 2 & \text{otherwise} \end{cases}$$

Having defined this metric d_{arch} , we define the metric on mappings as:

$$d(m_1, m_2) = d((m_1(k_1), \dots, m_1(k_{|K|})), (m_2(k_1), \dots, m_2(k_{|K|})))$$

$$= \sum_{i=1}^{|K|} |d_{\text{arch}}(m_1(k_i), m_2(k_i))| \quad (4)$$

For example, the distance between the orange mapping $m_1 \hat{=} (14, 15)$ and the dark-blue mapping $m_2 \hat{=} (7, 7)$ in Figure 7 is:

$$d(m_1, m_2) = |d_{\text{arch}}(14, 6)| + |d_{\text{arch}}(7, 7)| = 2 + 2 = 4$$

On the other hand, the distance between the dark-blue and the light-blue mapping is $2 + 1 = 3$

4.3.2 *Norm*. We selected the $p = 1$ norm for applying DC to mappings. For a finite-dimensional real space, the L_1^n norm is simply:

$$\|(x_1, \dots, x_n)\|_1 = \sum_{i=1}^n |x_i|$$

On a discrete space, this norm is commonly referred to as the ‘‘Manhattan’’ norm, and it corresponds to the metric on M from Equation 4. We believe out of the L_p norms, this one best captures the distance between processing elements.

4.4 The oracle

As explained above, the DC algorithm works using an oracle. It has a very simple specification: given a mapping $m \in M$, say if the encoded mapping $\text{encode}(m)$ is in the feasible set A ($\text{encode}(m) \in A \subseteq \{1, \dots, |R|\}^{|K|} \subseteq \mathbb{R}^n$). Whether a mapping is feasible depends on the user constraints (see Figure 2), e.g., number of resources, maximum energy consumption, or overall performance. As mentioned before, we only consider a single time bound t_0 :

We say a mapping m is *feasible* \Leftrightarrow

the time t from the simulation is below t_0

Thus, defining an oracle is simple: given a mapping m , it will run the simulator (c.f. II in Figure 4) and return feasible if the simulated time is $\leq t_0$. Note that the DC algorithm works on \mathbb{R}^n , whereas our encoding is a function in $\{1, 2, \dots, |R|\}^n$, a finite and discrete set. To deal with this, we round all coordinates of an $x \in \mathbb{R}^n$ to the nearest integer and let the oracle return infeasible if it falls outside the defined set. With this method, however, we neglect some information about A we already possess, namely, that it is a subset of $\{1, 2, \dots, |R|\}^n$. In future work we plan to address this by formulating a discrete (finite) version of the DC algorithm.

Consider again the example from Figure 7. For this very simple application, since the design-space is two-dimensional, we can

actually visualize it. If we let the application execute on every one of the $16^2 = 256$ mappings in this example, we get the heatmap depicted in B, where the color corresponds to the execution time. We see where the three mappings from A correspond to through the dotted lines. If we set the oracle function to use the time $t_0 = 80\text{ms}$, then the feasible space A will be the orange squares, whereas for $t_0 = 160\text{ms}$, it will encompass everything except the dark-blue diagonal.

5 EVALUATION

In this section we evaluate our approach, using three embedded applications on the architectures described in Section 4.2. The goal of the evaluation is twofold. First we want to generate a mapping with the DC approach from an initial mapping. This mapping was optimized with the conventional mapping tool flow of the SLX Tool Suite. Second we want to verify the robustness of the mapping obtained with the DC algorithm in comparison to the initial mapping and a set of randomly generated mappings. To this, we introduce perturbations to the mapping and check to what extend application constraints are still met. The perturbations correspond to local remapping decisions, emulating what operating system would do if it cannot deploy the statically computed mapping.

5.1 Applications

For testing, we use three applications from the signal processing and multimedia domains. The first one is an audio filter in the frequency domain. This filter processes a stereo audio signal from an input file of 16 bit samples at 48 kHz. It is functionally the same as the one presented in Figure 7, but split in 8 processes to expose more parallelism. The second application is a multiple input, multiple output orthogonal frequency division multiplexing (MIMO-OFDM) algorithm, similar to those used for 4G wireless communication. The code of the benchmark operates on randomly generated packets. The last application is a Sobel filter from the image processing domain.

5.2 Search Strategy

During the design-centering exploration, as part of the algorithm, we vary the radius of the L_p -ball. We achieve this by changing the hitting probability p during the iterations of the algorithm. Constrained to a small hitting probability, the DC algorithm tends to enlarge the sample region and vice versa. For the experiments we specify the following list of target hitting probabilities at different iterations (S) of the DC algorithm:

$$p = \begin{cases} 0.05 & \text{for } 0 < S \leq 15000 \\ 0.5 & \text{for } 15001 < S \leq 18750 \\ 0.75 & \text{for } 18751 < S \leq 22500 \\ 0.8 & \text{for } 22501 < S \leq 26250 \\ 0.95 & \text{for } 26251 < S \leq 30000 \end{cases}$$

The adaptation of the radius and the sampled hitting probability is illustrated in Figure 8, which shows a run of the DC algorithm for the MIMO-OFDM application. For the first half of the samples the hitting probability is fixed to $p = 0.05$, which forces the algorithm to increase the search radius in order to reach the target hitting probability p . After the first 15,000 samples, p decreases steadily and

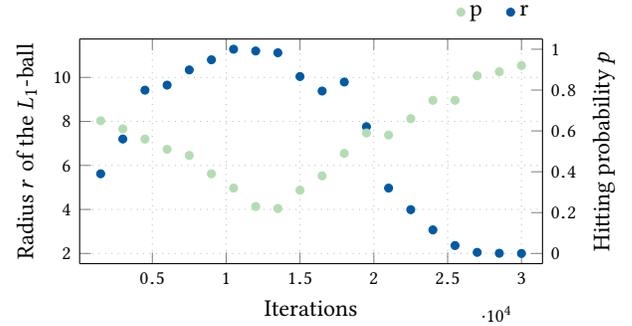


Figure 8: Radius and hitting probability of the L_1 -ball during a DC algorithm run

forces a smaller radius of the L_p -ball. Finally, a value of $p = 0.95$ with the last samples is reached. This strategy ensures that the calculated design center is located within a large feasibility region and does not get stuck on a local maximum.

Besides the dynamic adaptation of the search radius, the shape of the L_p -ball is also decisive for an exact hypervolume approximation. As mentioned before, we use the Manhattan metric as distance metric for the hypervolume. This is a good fit since we work on a 2-dimensional grid of PEs. The minimum radius (r_{\min}) of the L_1 -ball was set to one and the maximum to the half of the parameter space $r_{\max} = |K| \cdot |\{PE_i\}| / 2$, with $|K|$ being the dimension of the mapping vector (number of tasks) and $|\{PE_i\}|$ the number of PEs.

5.3 Results

In order to assess the robustness of the resulting mappings, we designed a perturbation method for testing it. The idea is to test whether a mapping still works within the given constraints after the static mapping is slightly changed. The modification of a single mapping m is performed by randomly perturbing the parameter vector $encode(m)$. For this, three random cores are chosen from the mapping and replaced by a different core of the given architecture. Our perturbation analysis consists in obtaining 100 modified versions of the original mapping $encode(m)$ and testing how many of those still meet the constraints. Note that the modifications of the vector are carried out without further consideration of the architecture. This means that a different core was selected without consideration of cluster boundaries or other communication infrastructures. In doing so, it was taken into account that some small changes of the mapping may result in a large impact on the run-time while others have very little effect. However, we believe those extrema are leveled out by the large number of perturbations. Thus, the robustness of different mappings is still comparable with this method.

To evaluate how robust the mapping computed with our approach really is, we also perform the perturbation analysis on other 199 feasible mappings obtained with the mapping flow. Figures 9–11 show the results of the perturbation analysis for the three applications on both target architectures. In the figures, the mappings (on the x-axis) are sorted according to robustness, i.e., what percentage of the 100 variations still meet the constraints. The mapping obtained with the DC approach and the first mapping computed

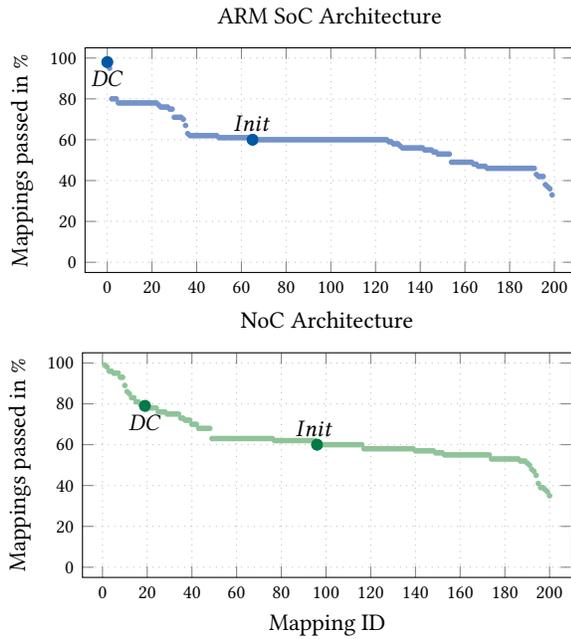


Figure 9: Perturbation charts for MIMO-OFDM benchmark on different architectures

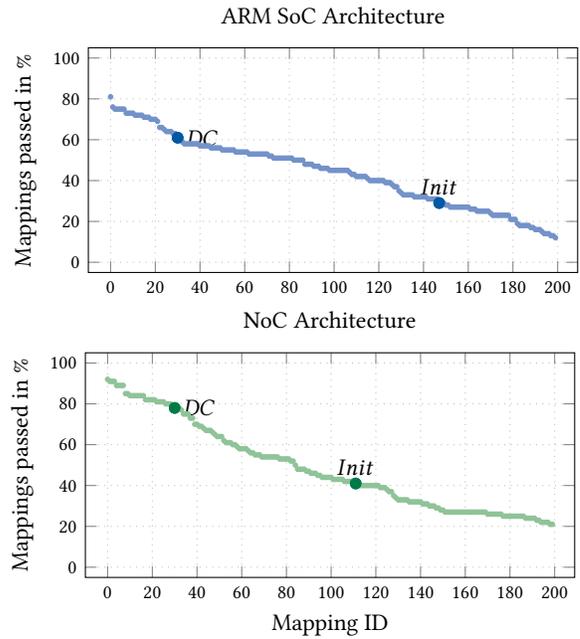


Figure 11: Perturbation charts for the Sobel filter benchmark on different architectures

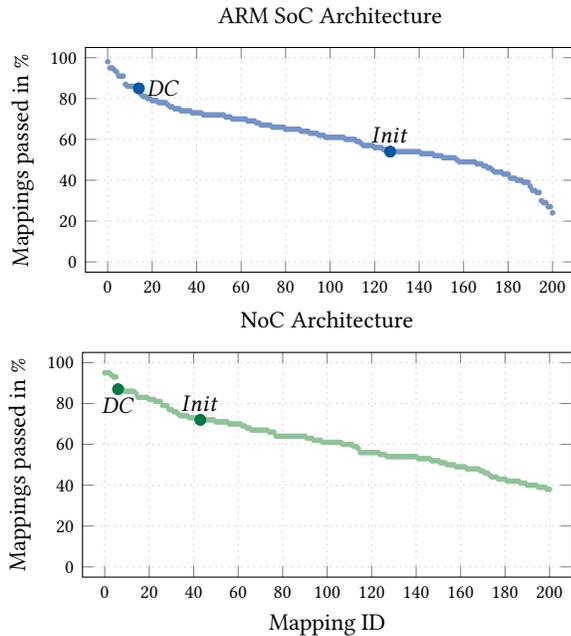


Figure 10: Perturbation charts for the Audio-Filter benchmark on different architectures

during the exploration (step I in Figure 4) are marked as "DC" and "Init" respectively. We see that in all instances, the mapping selected by the DC algorithm is in the first two deciles, and is, indeed, a very robust mapping. In particular, the results of the perturbation analysis for all three applications (Figure 9–11) imply that the

found design centers provide a clear improvement of robustness in comparison to the optimized initial mapping. Nonetheless, the evaluated design centers are of different quality, while the center of the MIMO-OFDM benchmark seems to be very robust against hardware perturbations (98%), the remaining benchmarks provide centers from 87% to 61%. Thus, it is quite possible that the algorithm will determine a local center, which could be surpassed in its quality by some random mapping. An investigation of this effect revealed that the deviations are triggered by different starting values, which is a usual behavior for a heuristic-based algorithm.

The perturbation analysis described above is quite time consuming. We also analyze whether it is possible to determine the quality of the design center without carrying the detailed analysis. To this end, we investigate the relation between the estimated hypervolume ("radius") of the feasible region with the quality (robustness). By construction, we expect said radius of the L_1 -balls of different design centers to correlate with the robustness of the mappings. We compared different design centers from the MIMO-OFDM benchmark on the ARM SoC with the described perturbation analysis (using identical random seeds for each center). The results of this, alongside a linear regression, are shown in Figure 12. Due to the small number of evaluated design centers (10), it is not clear how representative these values really are. However, the obtained results provide promising indications that there is a correlation between the size of the ascertained hypervolume and the quality of the results. A regression analysis also suggests a very high correlation (correlation coefficient of 0.984).

5.4 Limitations

The current version of the algorithm provides new samples as float types that have to be rounded to integer values. This procedure

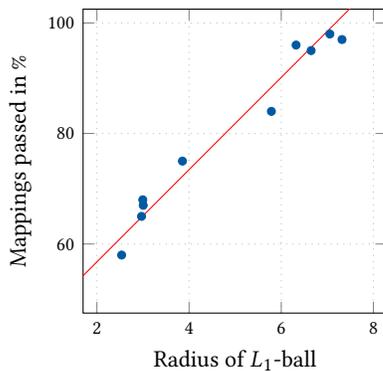


Figure 12: Correlation between radius of the L_1 -ball and robustness of the DC

results in multiple duplicate measurements as slightly different samples can be merged to identical mappings. In order to avoid repetitive simulations of mappings, an internal cache was implemented in the oracle function. This problem can only be solved by using an internal discretization of the DC algorithm. This adaption for discrete problems is part of the ongoing development of the design DC algorithm.

6 RELATED WORK

This section introduces previous works that are related to the problem of adaptive dynamic mapping for changed hardware or software constraints. Typically, dynamic mapping of process networks or tasks graphs is necessary for multiple tasks running on multicores on an embedded operating system.

This problem is sometimes solved by holding multiple static schedules calculated at compile time of the application, e.g. [20, 28, 49]. As this requires comprehensive knowledge of all possible system states, these approaches suffer from a bad scalability. Thus, several attempts were made to provide light-weight run-time mappings for process networks. Most of this approaches use a twofold strategy: computing parts of the mapping at compile time and make the final adaptations to the mapping at runtime. Examples for such hybrid approaches can be found in [9, 33, 47].

In order to provide these compile time optimized mappings for different usage scenarios a comprehensive design space exploration is required. This issue has been extensively studied in recent years, e.g. [32] tries to find Pareto fronts within the design space of a data-flow application, or [40] describes an exploration methodology for multi-objective constraints. In general, it is difficult to compare these mapping approaches [15].

However, most of the hybrid approaches for dynamic mapping either run into scalability problems as they provide only static parts or require considerable computing resources at runtime. Our idea was to decrease the computational effort at runtime to nearly zero by providing a mapping that can be modified within certain boundaries without affecting the given constraints of the application. Therefore, we used a design centering approach as it is commonly used in integrated-circuit design [7] and material sciences [30]. Our approach requires also a design space exploration at compile-time but uses the gathered information to provide a robust design. To

the best of our knowledge, we are the first using design centering for the development of robust mapping in the context of dataflow applications.

7 CONCLUSIONS AND PERSPECTIVE

We described an application of a bio-inspired design centering algorithm to compute robust mappings for multicores. In contrast to conventional optimization methods, the applied algorithm does not try to find one distinct optimal point, but rather a whole region that fulfills a certain condition. For this purpose, the design centering algorithm explores the design space in order to find a point which is in the center of a determined hypervolume of points that meet the given constraints. In this work, the algorithm was used to find mappings that provided a certain degree of robustness against slight remapping changes during runtime. We believe design centering can be used to generate mappings that are robust to other kinds of perturbations, and that this is an interesting area of research.

To evaluate our approach we used a state-of-the-art tool flow for mapping KPN applications to multicore architectures. We performed a perturbation analysis for three applications onto two fundamentally different architectures. Compared to conventionally optimized mappings, the generated mappings turned out to be $\approx 29\%$ more robust against changes of hardware resources.

In future work, we will specialize the design centering algorithm to be directly applied to discrete problems. Furthermore, we are planning to apply the algorithm to other problems from the field of process network optimizations, e.g., mapping robustness with respect to changes in the internal control flow of the processes.

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