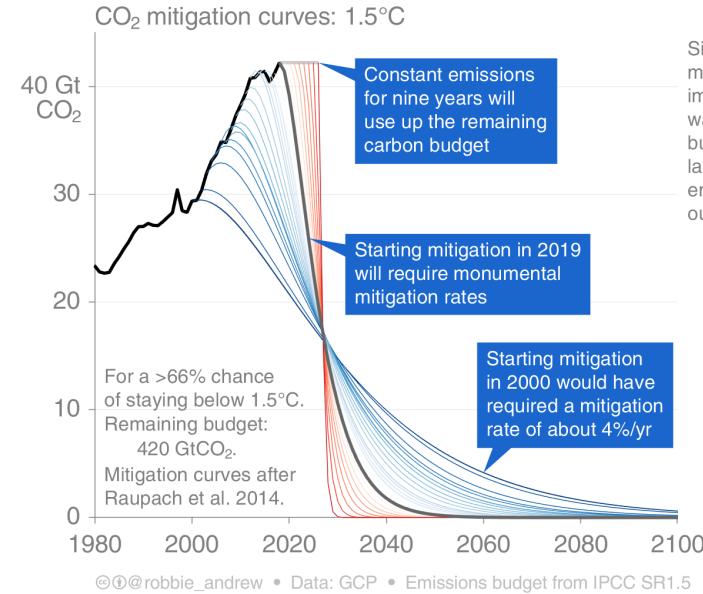


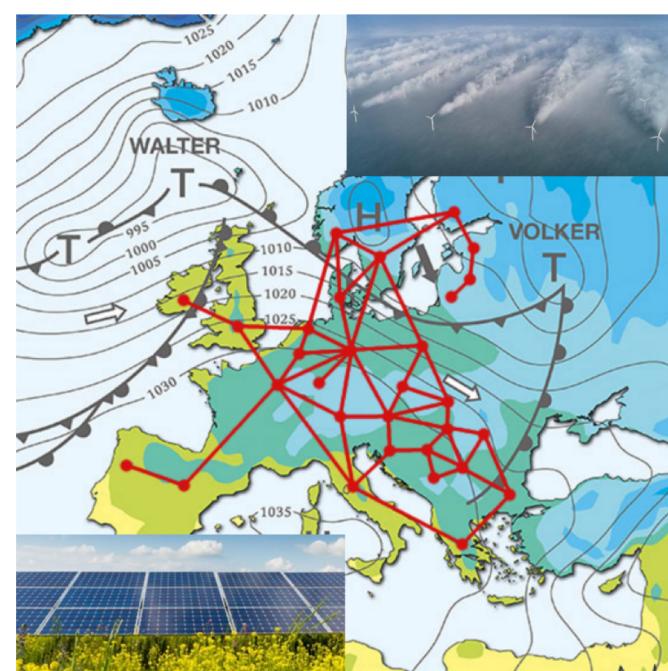
Decarbonisation of the networked European Energy System

- I. **simple modeling: Renewable European electricity network**
 - weather-driven optimal design
 - value of cooperation

- II. **advanced modeling:
electricity → energy network**
 - constraints
 - + (unavoidable) consequences



Since such steep mitigation is impossible, the only way to achieve this budget is with very large "negative" emissions: pulling CO₂ out of the atmosphere.



Flow tracing and nodal cost allocation in renewable energy networks

E Eriksen, L Schwenk-Nebbe, B Tranberg, T Brown, M Greiner:

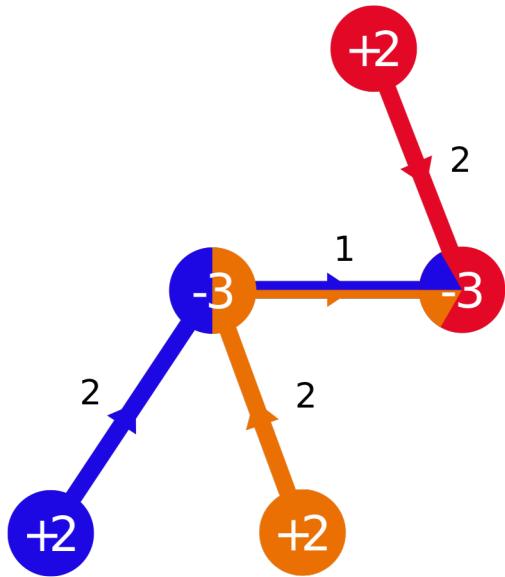
Optimal heterogeneity in a simplified highly renewable European electricity system

Energy 133 (2017) 913-28.

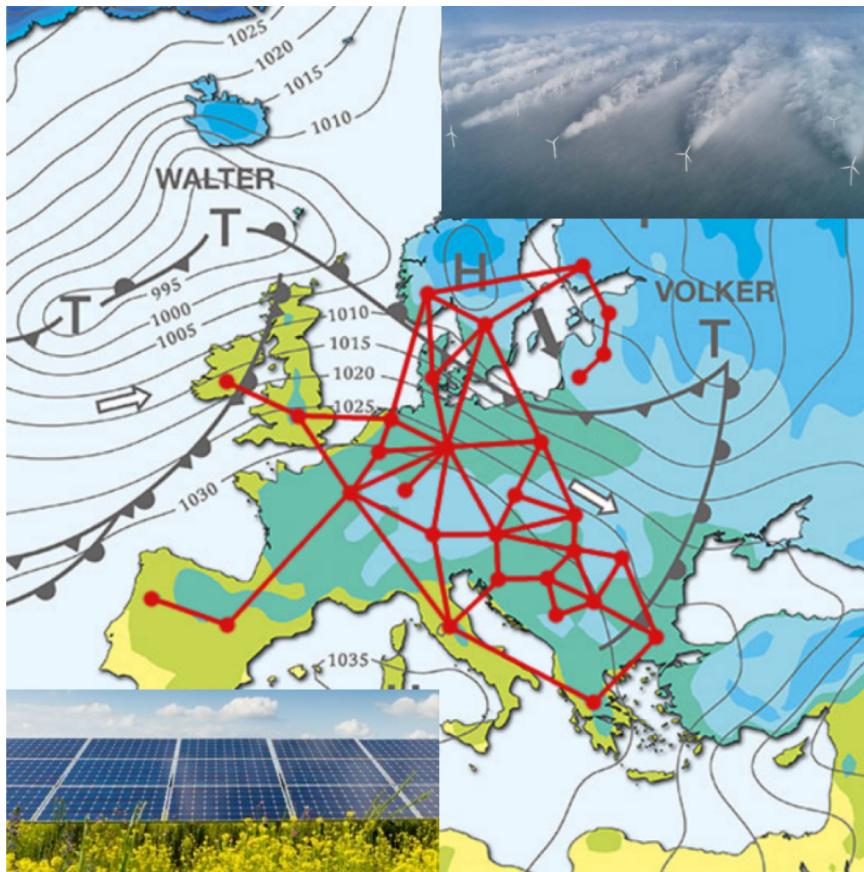
B Tranberg, L Schwenk-Nebbe, M Schäfer, J Hörsch, M Greiner:

Flow-based nodal cost allocation in a heterogeneous highly renewable European electricity system

Energy 150 (2018) 122-33.



I. Simple Modeling: Renewable European electricity network



**Design of energy systems with
a high share of renewables:**

Let the weather decide!



Renewable European electricity network + fluctuating „weather forces“

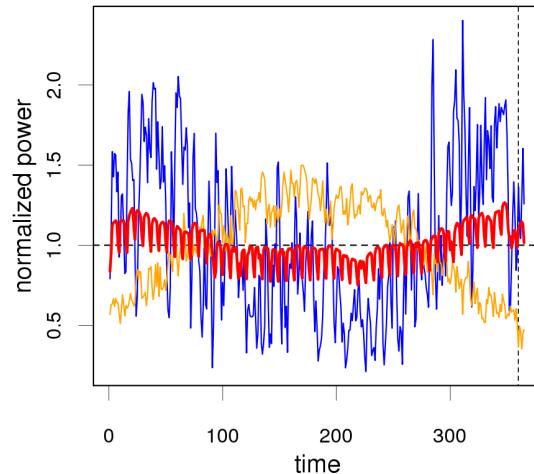
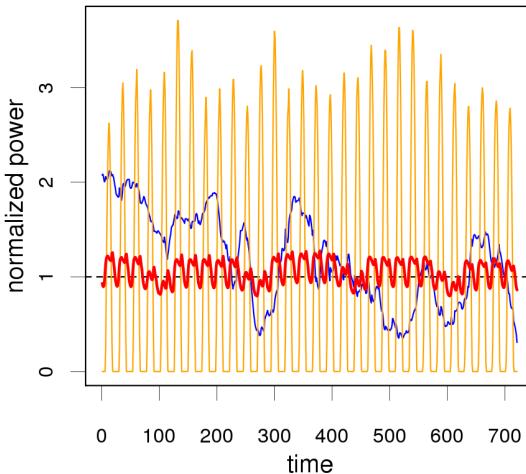
$$G_n^R(t) = G_n^W(t) + G_n^S(t)$$

$$\langle G_n^R \rangle = \gamma_n \langle L_n \rangle$$

$$\langle G_n^W \rangle = \alpha_n \langle G_n^R \rangle$$

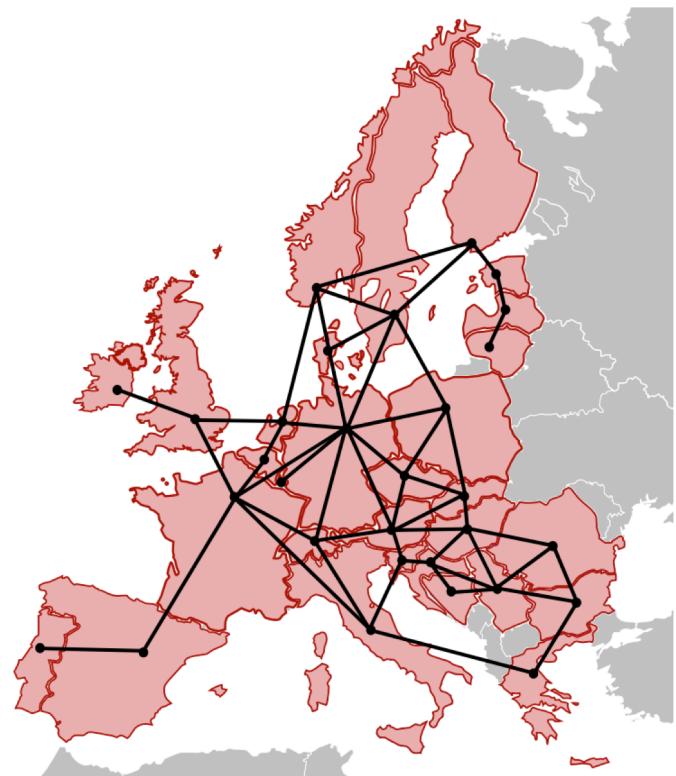
1980 – 2018: 1h, 30x30km²

Renewable Energy Atlas



3 TIME SCALES:

diurnal
synoptic
seasonal (1h-1d)
 (2-10d)
 (1y)



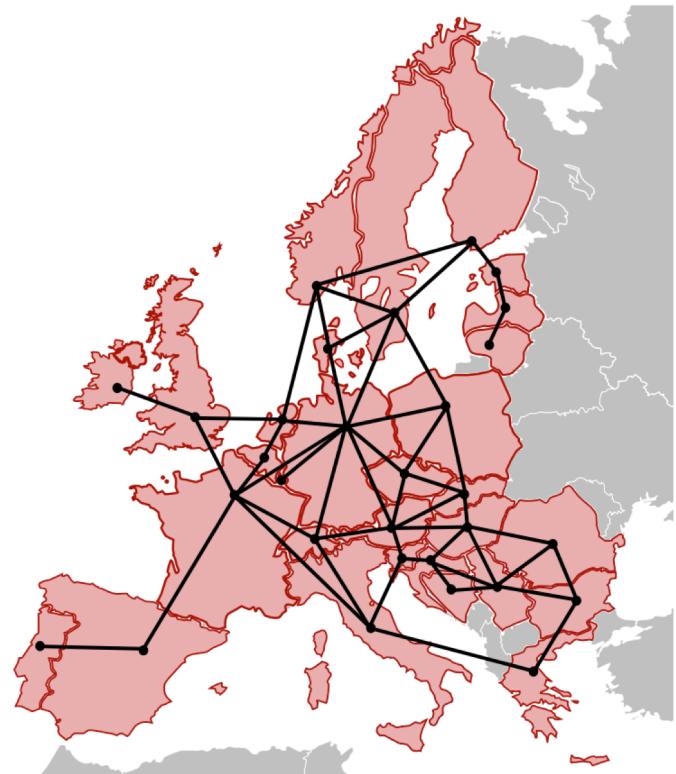
Renewable European electricity network + fluctuating „weather forces“

$$G_n^R(t) = G_n^W(t) + G_n^S(t)$$

$$\langle G_n^R \rangle = \gamma_n \langle L_n \rangle$$

$$\langle G_n^W \rangle = \alpha_n \langle G_n^R \rangle$$

$$G_n^R(t) - L_n(t) = B_n(t) + P_n(t) + \dots$$



Renewable European electricity network + fluctuating „weather forces“

$$G_n^R(t) = G_n^W(t) + G_n^S(t)$$

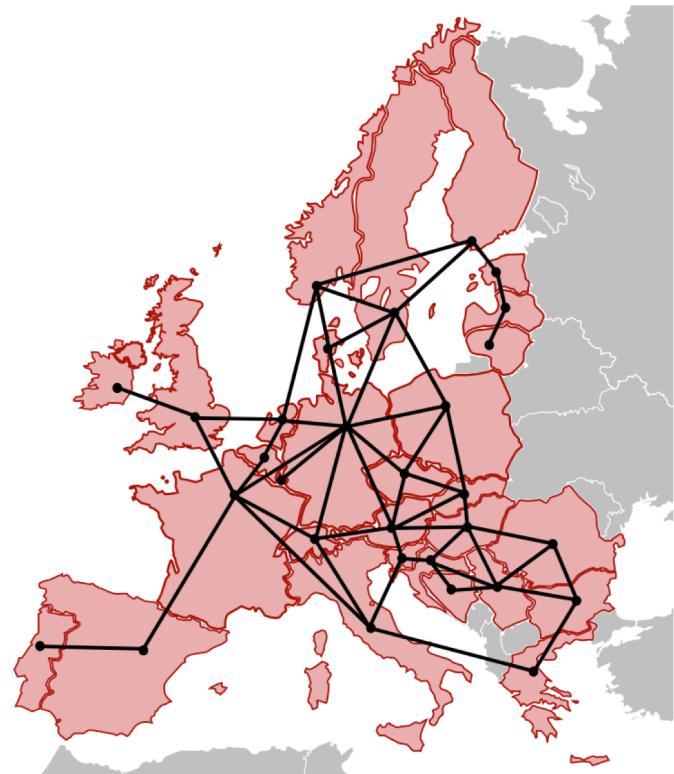
$$\langle G_n^R \rangle = \gamma_n \langle L_n \rangle$$

$$\langle G_n^W \rangle = \alpha_n \langle G_n^R \rangle$$

$$G_n^R(t) - L_n(t) = B_n(t) + P_n(t) + \dots$$

$$G_n^B(t) = (B_n(t))_-$$

$$C_n(t) = (B_n(t))_+$$



Renewable European electricity network + fluctuating „weather forces“

$$G_n^R(t) = G_n^W(t) + G_n^S(t)$$

$$\langle G_n^R \rangle = \gamma_n \langle L_n \rangle$$

$$\langle G_n^W \rangle = \alpha_n \langle G_n^R \rangle$$

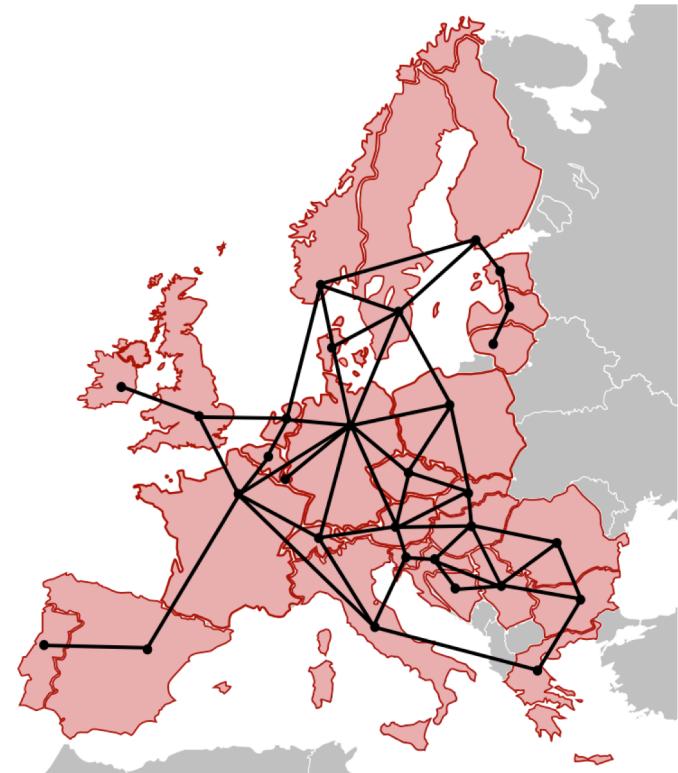
$$G_n^R(t) - L_n(t) = B_n(t) + P_n(t) + \dots$$

$$G_n^B(t) = (B_n(t))_-$$

$$C_n(t) = (B_n(t))_+$$

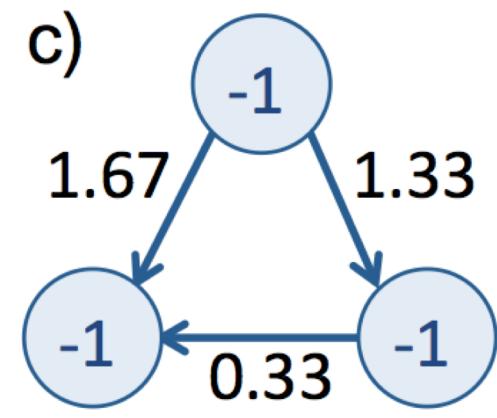
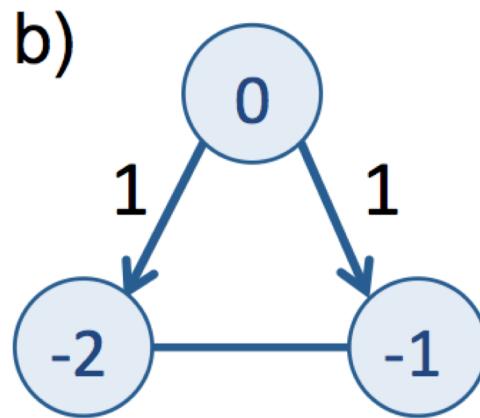
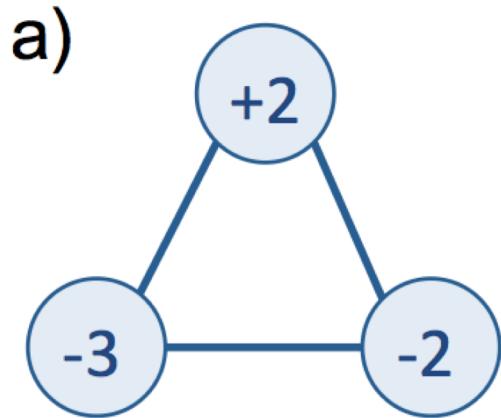
$$\sum_n P_n(t) = 0$$

$$F_l(t) = \sum_n H_{ln} P_n(t)$$



“interactions”: balancing \leftrightarrow transmission

$$\Delta_n(t) = G_n^R(t) - L_n(t) = B_n(t) + P_n(t)$$



$$P_n(t) = 0$$

$$\min\left(\sum_n G_n^B(t)\right)$$

$$\min\left(\sum_l F_l^2(t)\right)$$

$$B_n(t) = \beta(t) \langle L_n \rangle$$

$$\beta(t) = \frac{\sum_n \Delta_n(t)}{\sum_n \langle L_n \rangle}$$

Renewable European electricity network + fluctuating „weather forces“

$$G_n^R(t) = G_n^W(t) + G_n^S(t)$$

$$\langle G_n^R \rangle = \gamma_n \langle L_n \rangle$$

$$\langle G_n^W \rangle = \alpha_n \langle G_n^R \rangle$$

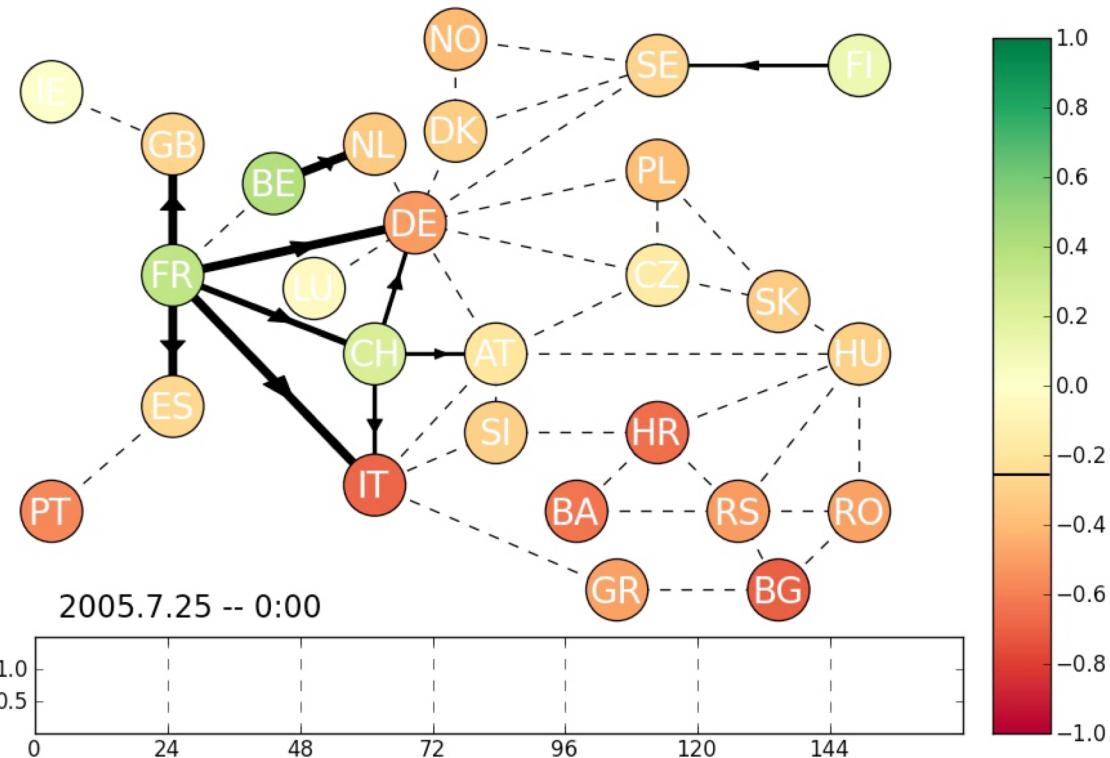
$$G_n^R(t) - L_n(t) = B_n(t) + P_n(t) + \dots$$

$$G_n^B(t) = (B_n(t))_-$$

$$C_n(t) = (B_n(t))_+$$

$$\sum_n P_n(t) = 0$$

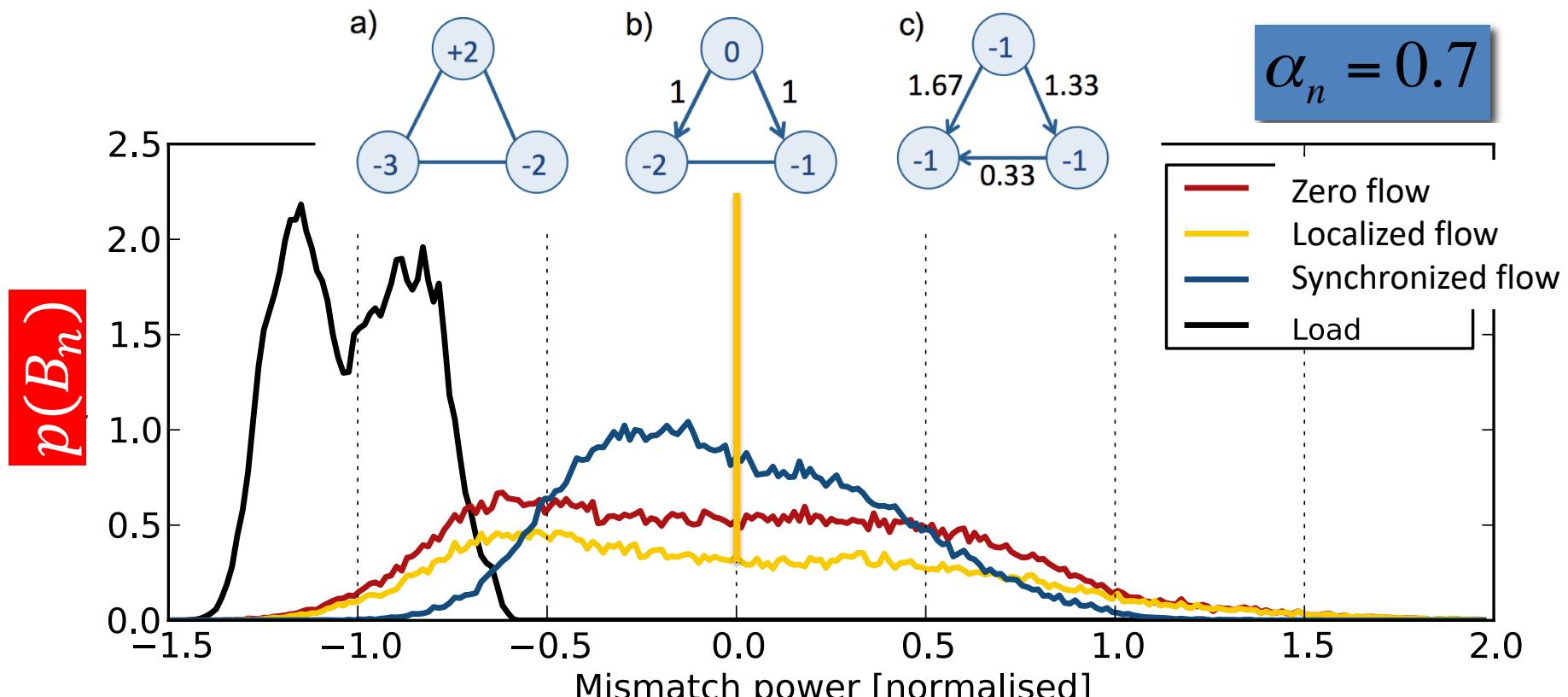
$$F_l(t) = \sum_n H_{ln} P_n(t)$$



Balancing distribution (Germany)

$$B_n(t) = G_n^{RES}(t) - L_n(t) - P_n(t)$$

$$\langle G_n^{RES} \rangle = \langle L_n \rangle$$



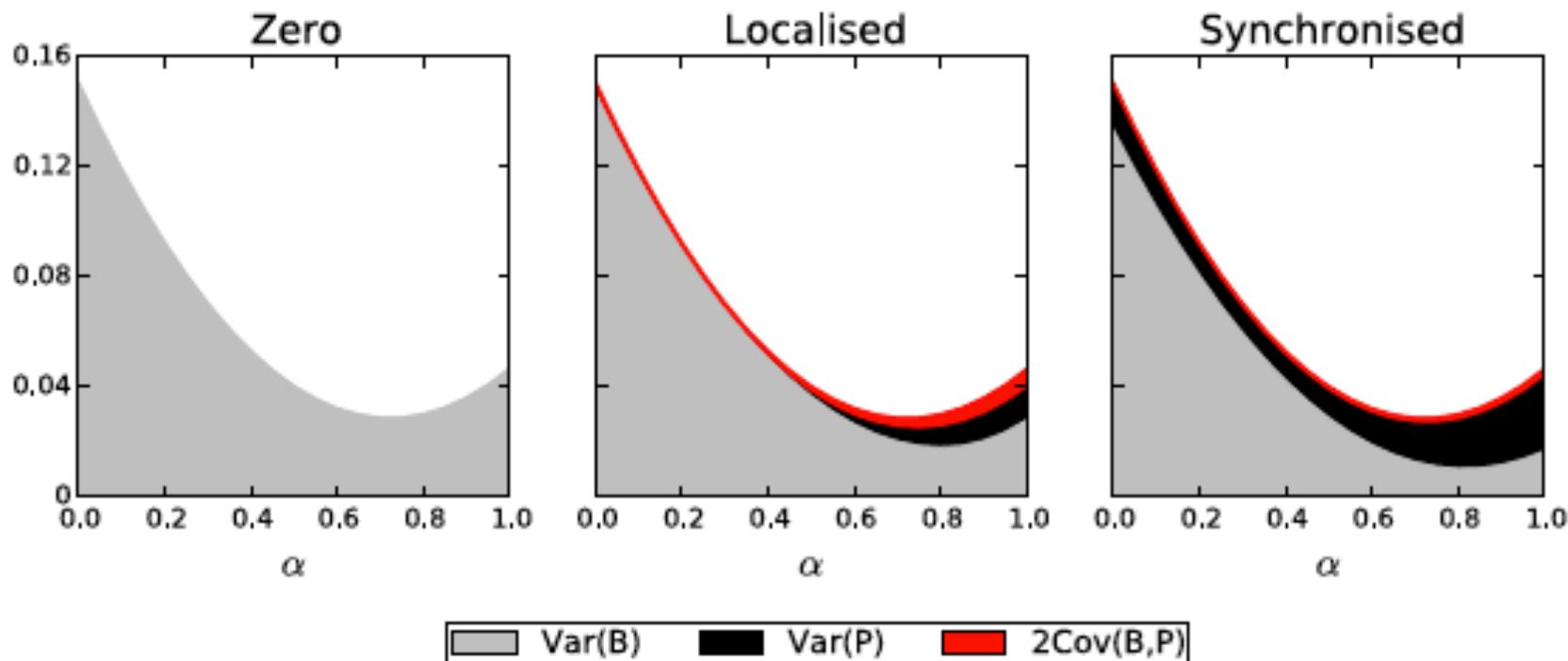
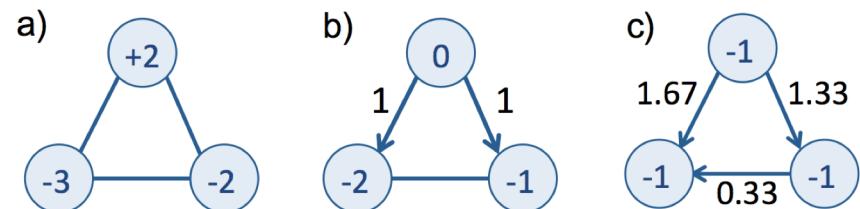
$$G_n^B(t) = (B_n(t))_-$$

$$C_n(t) = (B_n(t))_+$$



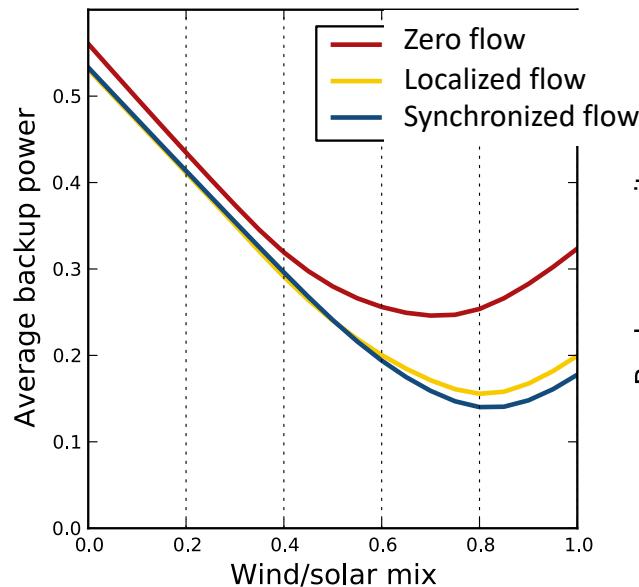
variance: balancing \leftrightarrow transmission

$$\begin{aligned}\Delta_n(t) &= \\ &= G_n^R(t) - L_n(t) \\ &= B_n(t) + P_n(t)\end{aligned}$$



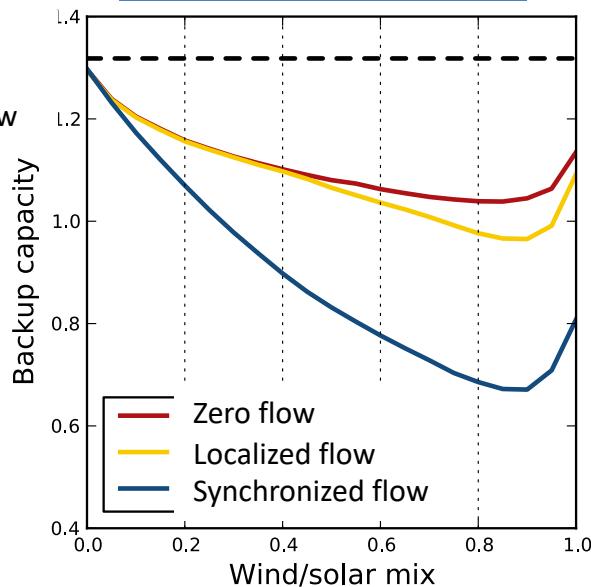
backup energy

$$\langle G_n^B \rangle$$



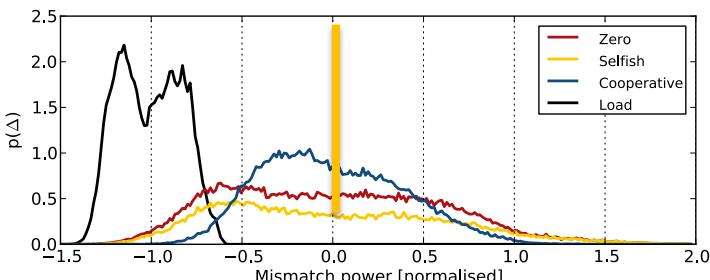
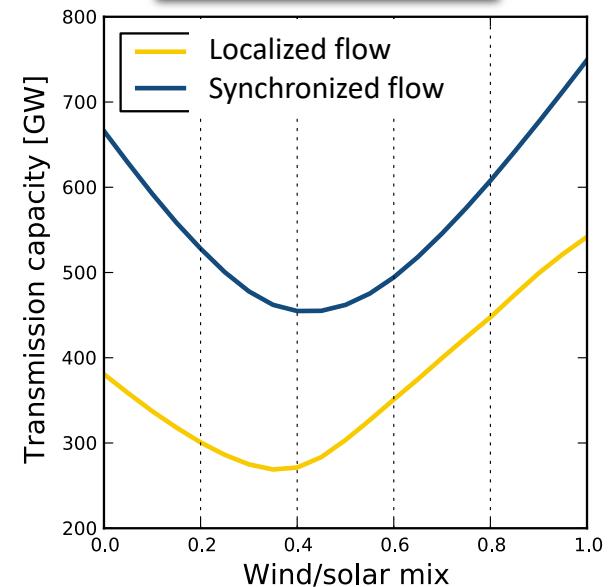
backup capacity

$$\max_q(G_n^B)$$

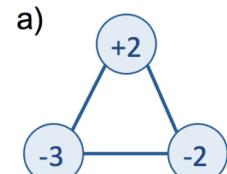


transmission capacity

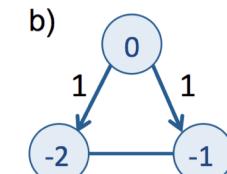
$$\sum_l \max_q |F_l|$$



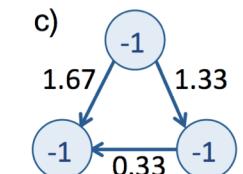
a)



b)



c)



Infrastructure measures

backup energy

$$E_n^B = \langle G_n^B \rangle$$

backup capacity

$$K_n^B = \max_q(G_n^B)$$

transmission capacity

$$K_l^T = \max_q |F_l| \cdot d_l$$

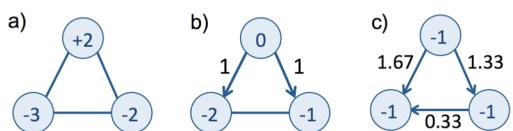
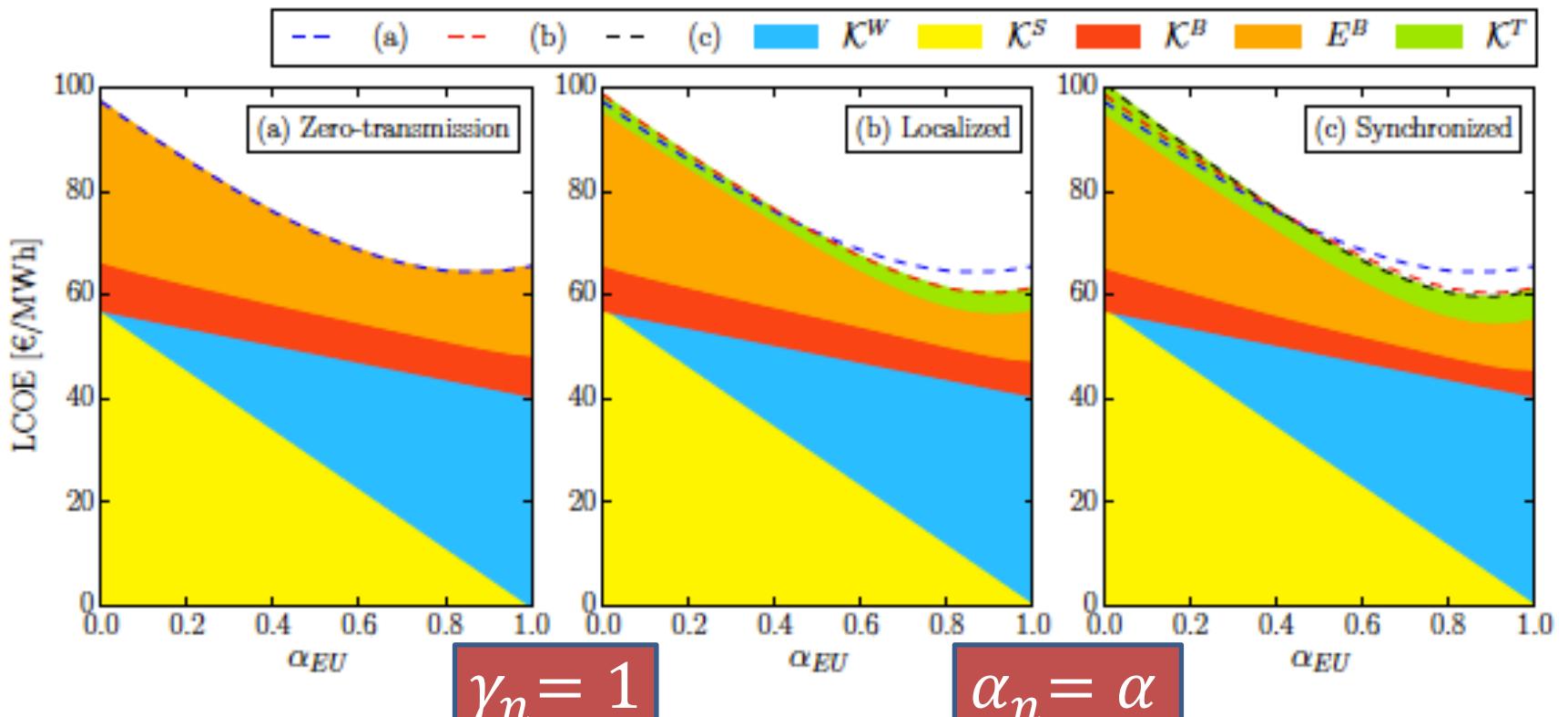
wind capacity

$$K_n^W = \frac{\alpha_n \gamma_n \langle L_n \rangle}{CF_n^W}$$

solar capacity

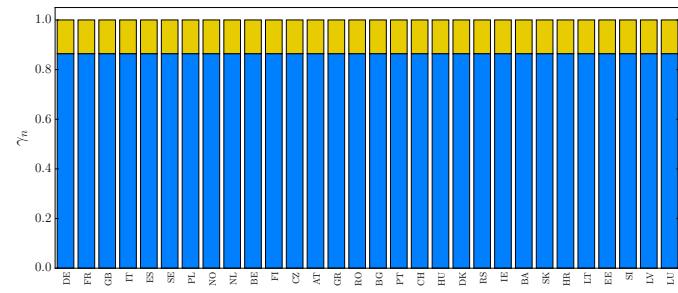
$$K_n^S = \frac{(1 - \alpha_n) \gamma_n \langle L_n \rangle}{CF_n^S}$$

Levelized Cost of SYSTEM Energy

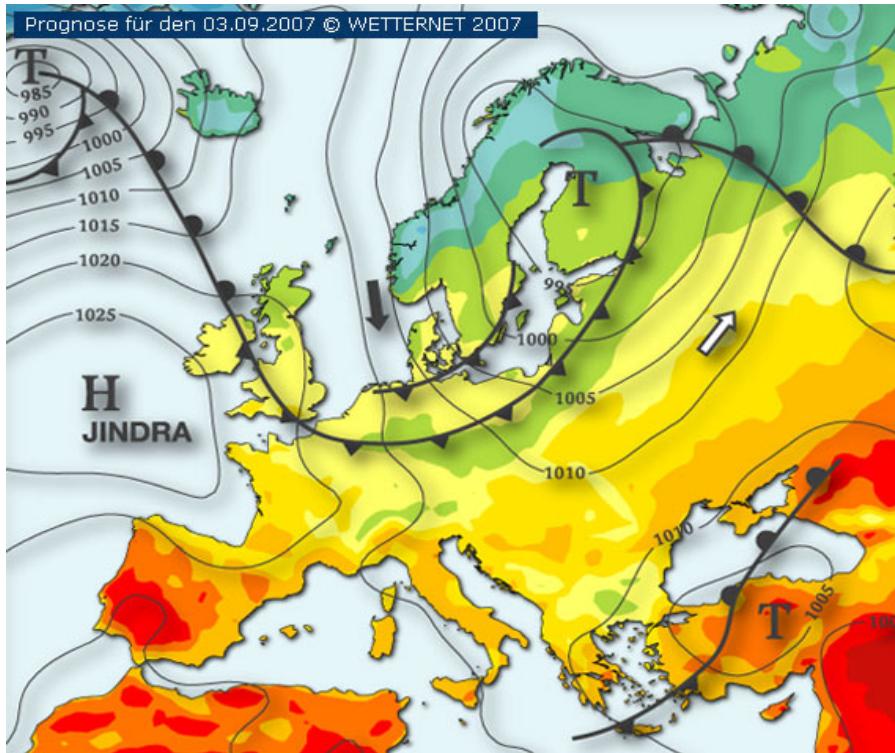


Coupling objectives: $B \leftrightarrow P$

$$G_n^R(t) - L_n(t) = B_n(t) + P_n(t)$$



wind and solar power capacities

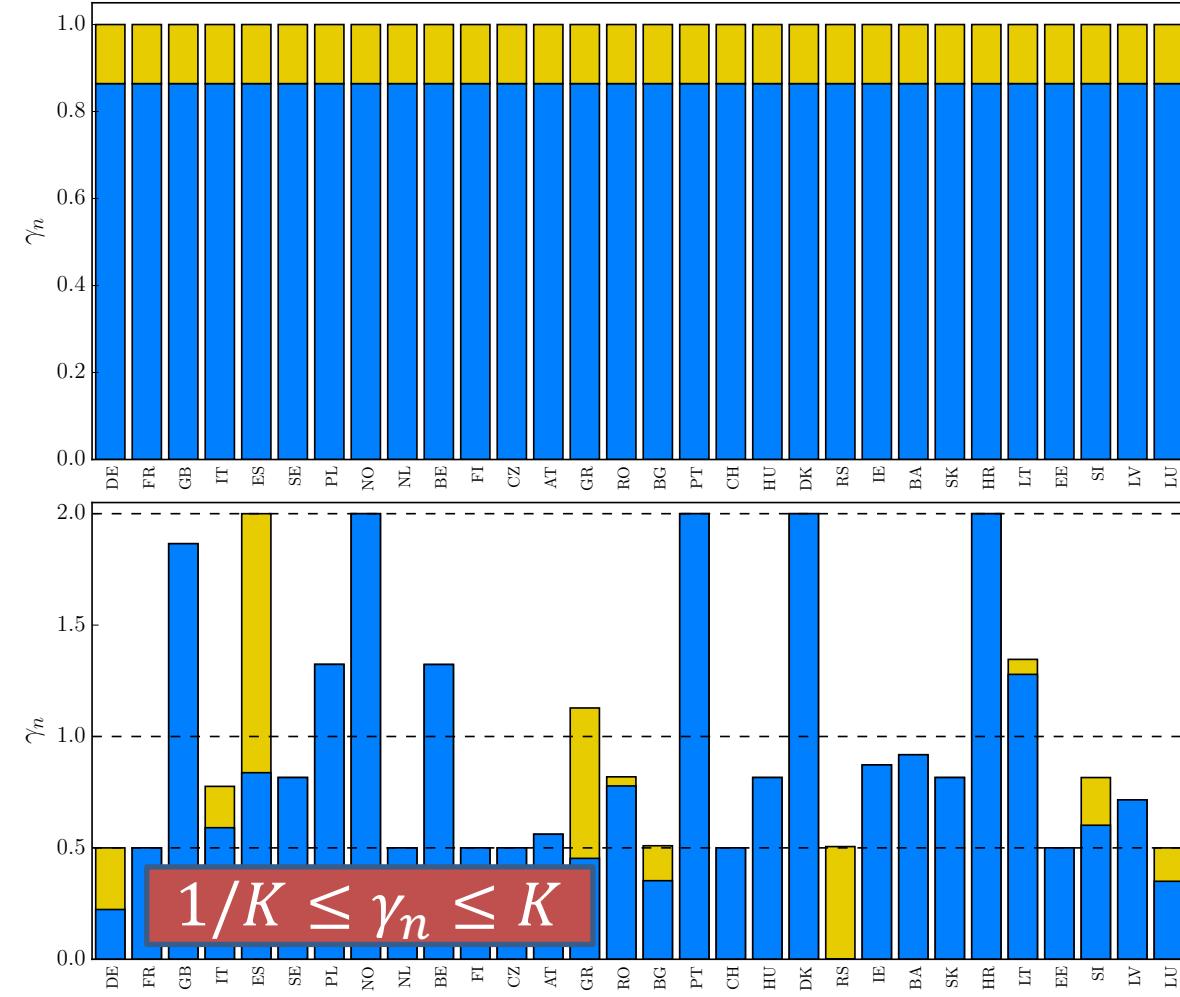


annual consumption (2009)
= 3400 TWh

80% wind power generation
= 1000 GW installed capacity
= 200.000 x 5 MW turbines
= 5000 x 200 MW wind farms
 $\approx 130000 \text{ km}^2$

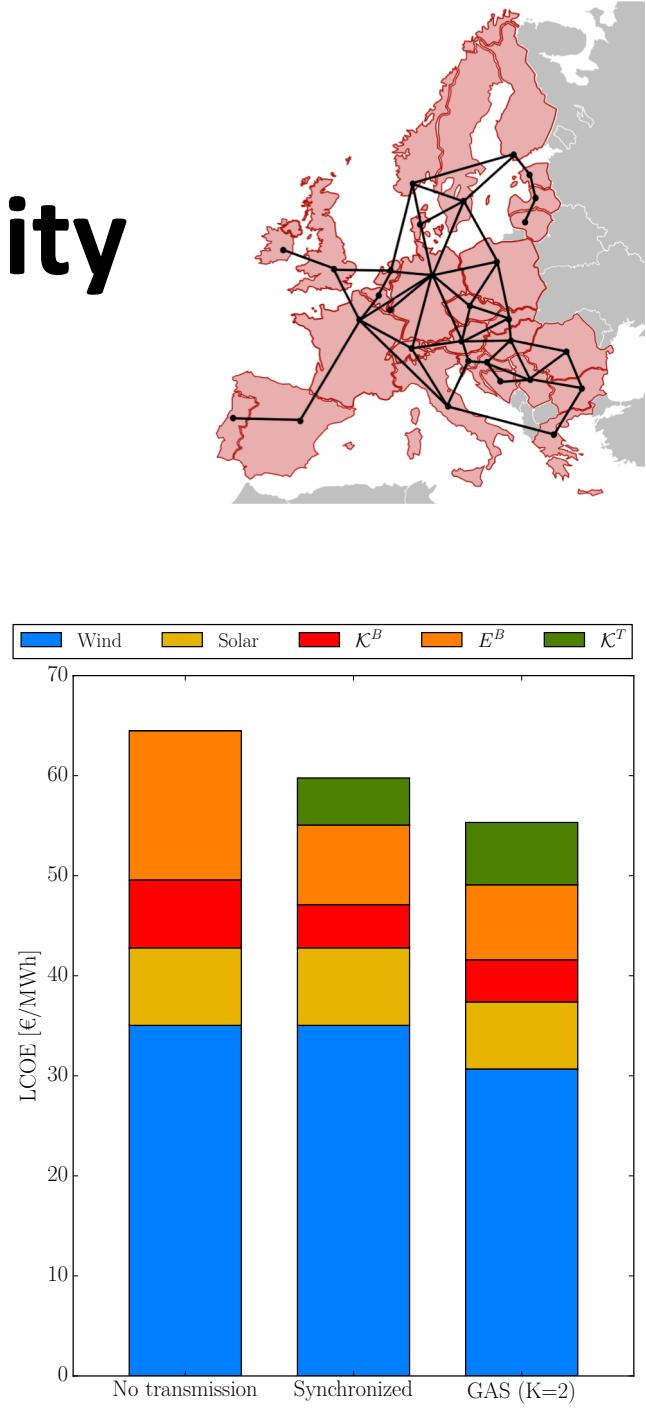
20% solar PV power generation
= 370 GW installed capacity
 $\approx 2500 - 5000 \text{ km}^2$

Breaking homogeneity: cost-optimal heterogeneity



$$\langle G_n^R \rangle = \gamma_n \langle L_n \rangle$$

$$\langle G_n^W \rangle = \alpha_n \langle G_n^R \rangle$$



Back-on-the-envelop estimate

OPT-HOM-noT(K=1):	64.5 €/MWh
OPT-HOM(K=1):	56.6 €/MWh
OPT-HET(K=2):	53.8 €/MWh

EU cost reduction / y

$$= 3500 \text{ TWh/y} \times 10 \text{ €/MWh}$$

$$= 35 \times 10^9 \text{ €/y}$$



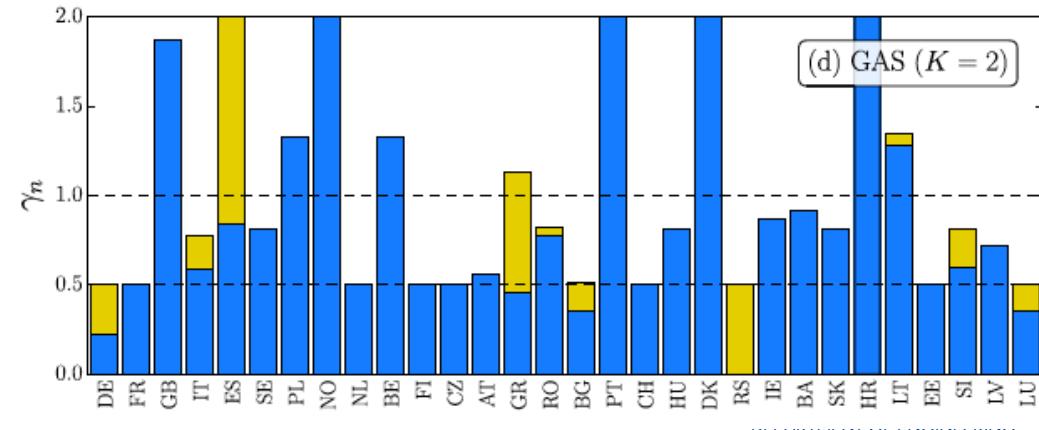
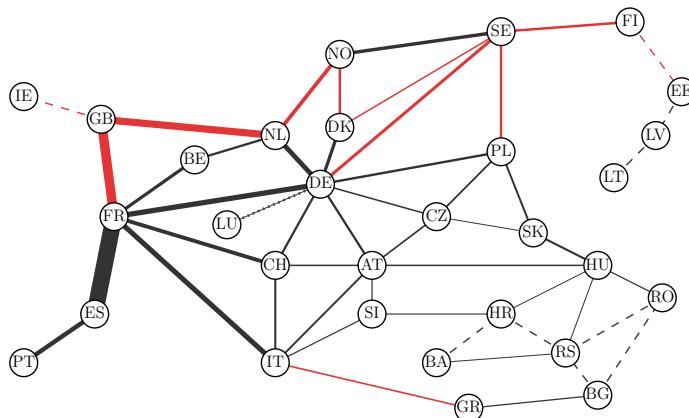
30 European friends you have to be!

but who pays for ...

..... the heterogeneity?

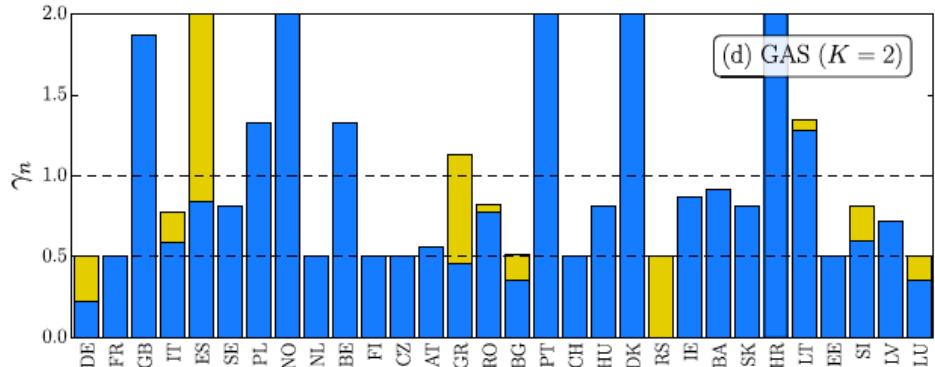
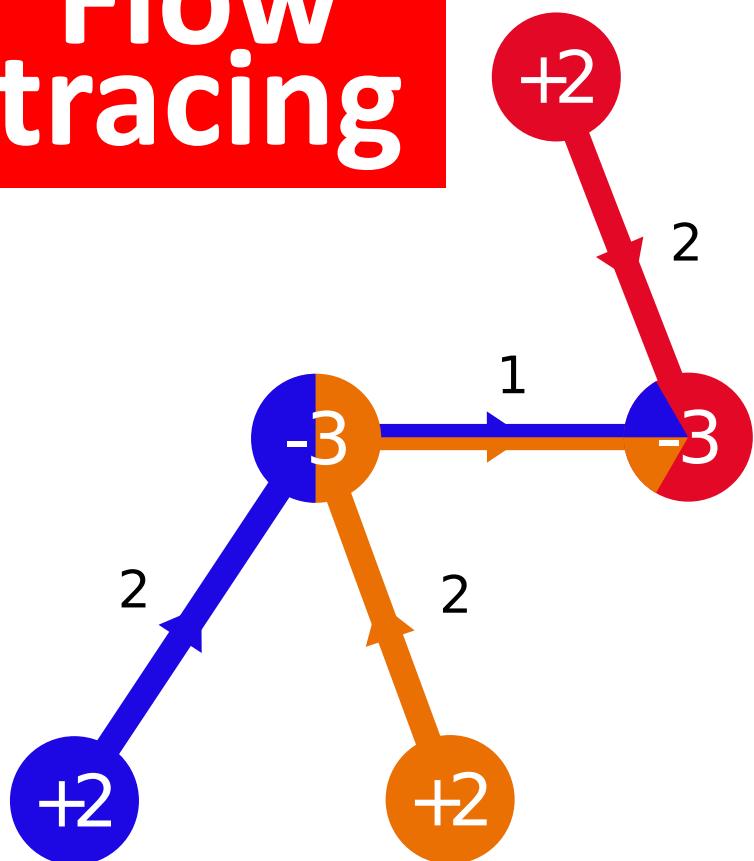
..... the transmission grid?

..... 0 – 2.5% - - - 2.5 – 5% — 10% — 25% — 50% — 100%



Who pays for the heterogeneity?

Flow tracing

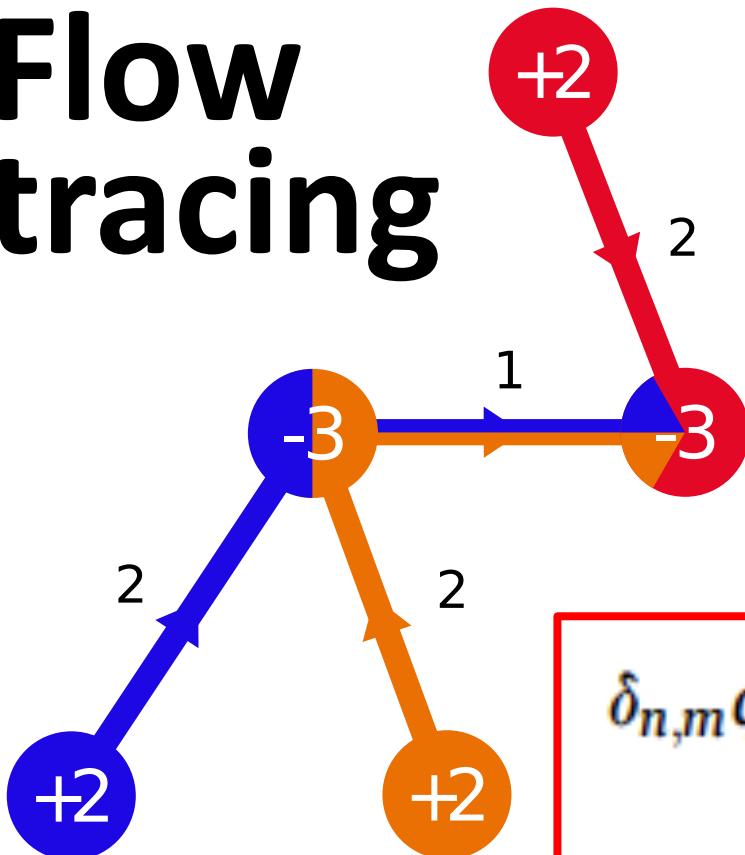


$$K_n^\mu = K_{nn}^\mu + \sum_{m \neq n} K_{nm}^\mu$$

$$\tilde{K}_n^\mu = K_{nn}^\mu + \sum_{m \neq n} K_{mn}^\mu$$



Flow tracing

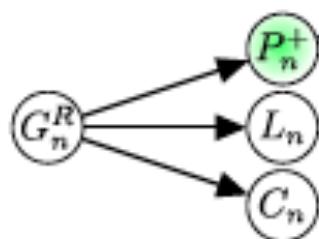


$$\begin{aligned} \delta_{n,m} q_{(n,\mu)}^{\text{in}} P_n^+ + \sum_k q_{k \rightarrow n, (m,\mu)} F_{k \rightarrow n} \\ = q_{n, (m,\mu)}^{\text{out}} P_n^- + \sum_k q_{n \rightarrow k, (m,\mu)} F_{n \rightarrow k}, \end{aligned}$$



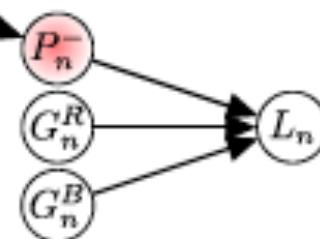
Export (a): $G_n^R > L_n, C_n > 0$

$$F_n^{\text{in}} \longrightarrow F_n^{\text{out}}$$



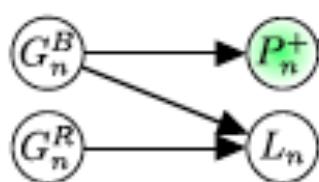
Import (d): $G_n^R < L_n, G_n^B > 0$

$$F_n^{\text{in}} \longrightarrow F_n^{\text{out}}$$



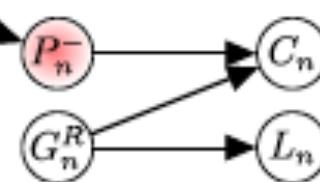
Export (b): $G_n^R < L_n, G_n^B > 0$

$$F_n^{\text{in}} \longrightarrow F_n^{\text{out}}$$



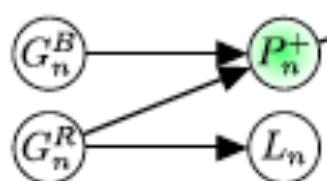
Import (e): $G_n^R > L_n, C_n > 0$

$$F_n^{\text{in}} \longrightarrow F_n^{\text{out}}$$



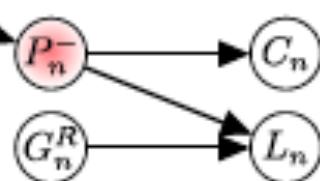
Export (c): $G_n^R > L_n, G_n^B > 0$

$$F_n^{\text{in}} \longrightarrow F_n^{\text{out}}$$

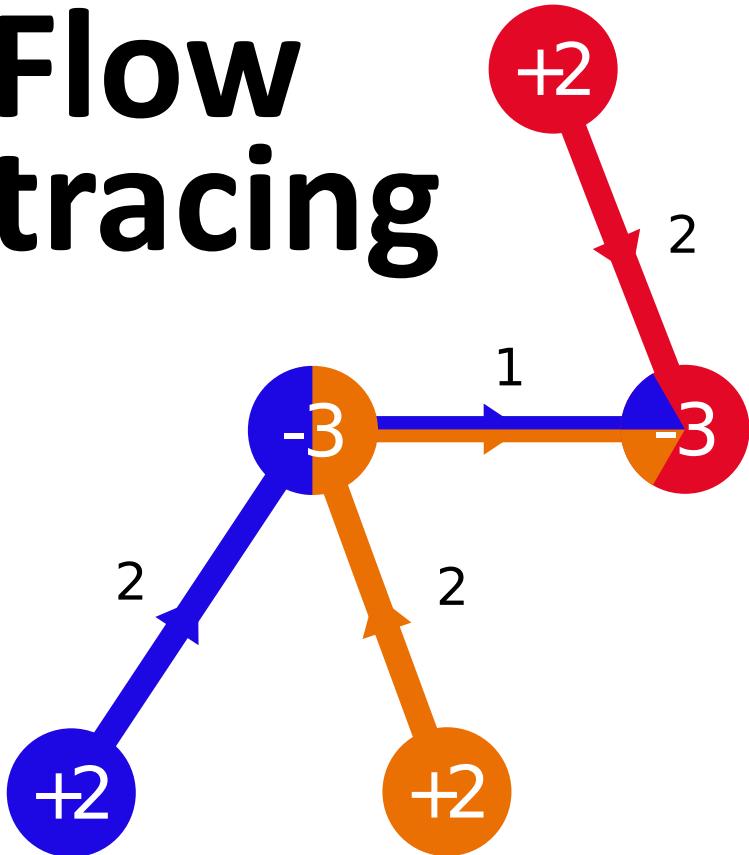


Import (f): $G_n^R < L_n, C_n > 0$

$$F_n^{\text{in}} \longrightarrow F_n^{\text{out}}$$



Flow tracing



$$\begin{aligned} & \delta_{n,m} q_{(n,\mu)}^{\text{in}} P_n^+ + \sum_k q_{k \rightarrow n, (m,\mu)} F_{k \rightarrow n} \\ &= q_{n, (m,\mu)}^{\text{out}} P_n^- + \sum_k q_{n \rightarrow k, (m,\mu)} F_{n \rightarrow k}, \end{aligned}$$

$$\mathcal{E}_{m \rightarrow n}^\mu = \langle q_{n, (m,\mu)}^{\text{out}} P_n^- \rangle.$$

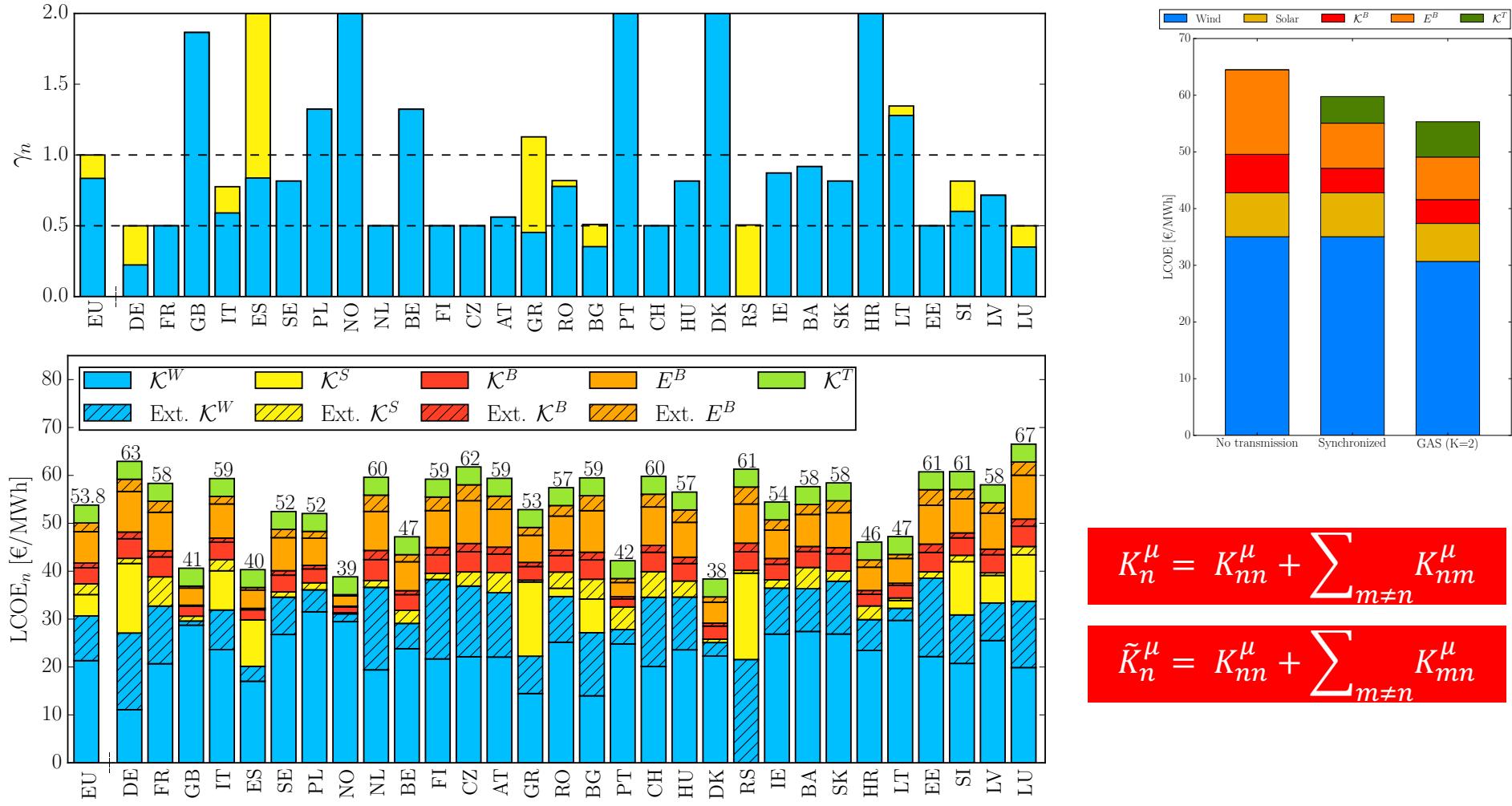
$$\mathcal{K}_{m \rightarrow n}^\mu = \begin{cases} \left[\frac{\mathcal{E}_{m \rightarrow n}^\mu}{\langle G_m^\mu \rangle - \langle C_m^\mu \rangle} \right] \mathcal{K}_m^\mu & \text{if } m \neq n \\ \mathcal{K}_m^\mu - \sum_{s \neq m} \mathcal{K}_{m \rightarrow s}^\mu & \text{if } m = n. \end{cases}$$

$$K_n^\mu = K_{nn}^\mu + \sum_{m \neq n} K_{nm}^\mu$$

$$\widetilde{K}_n^\mu = K_{nn}^\mu + \sum_{m \neq n} K_{mn}^\mu$$



Benefit of cooperation

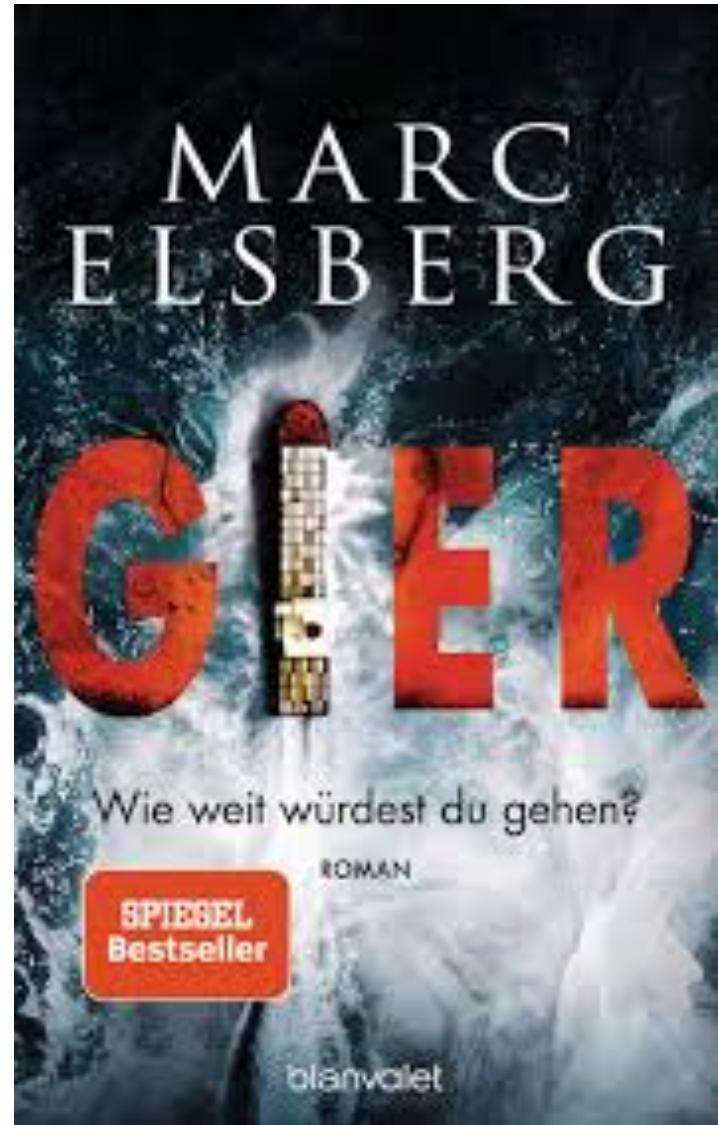
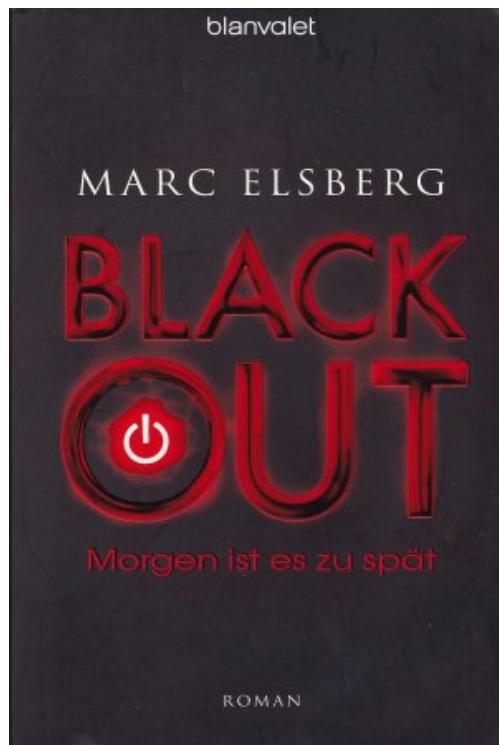


$$K_n^\mu = K_{nn}^\mu + \sum_{m \neq n} K_{nm}^\mu$$

$$\tilde{K}_n^\mu = K_{nn}^\mu + \sum_{m \neq n} K_{mn}^\mu$$

$\forall n: LCOE_n^{hom,notT} > LCOE_n^{hom,T} > LCOE_n^{het,T}$

30 EU friends
you have to be!



AARHUS
UNIVERSITY
DEPARTMENT OF ENGINEERING

“Gier” nach mehr Physik:

power-flow renormalization

M Schäfer et.al.,
EPL 119 (2017) 38004

storage phase transition

T Jensen + M Greiner,
EPJ ST 223 (2014) 2475-81

principal spatio-temporal patterns

M Raunbak et.al., Energies 10 (2017) 2934
F Hofmann et.al., EPL 124 (2018) 18005

mesoscale turbulence + climate change

M Schlott, A Kies et.al.,
Applied Energy 230 (2018) 1645-59

flexibility classes

D Schlachtberter et.al.,
Energy Conversion Management 125 (2016) 336-46



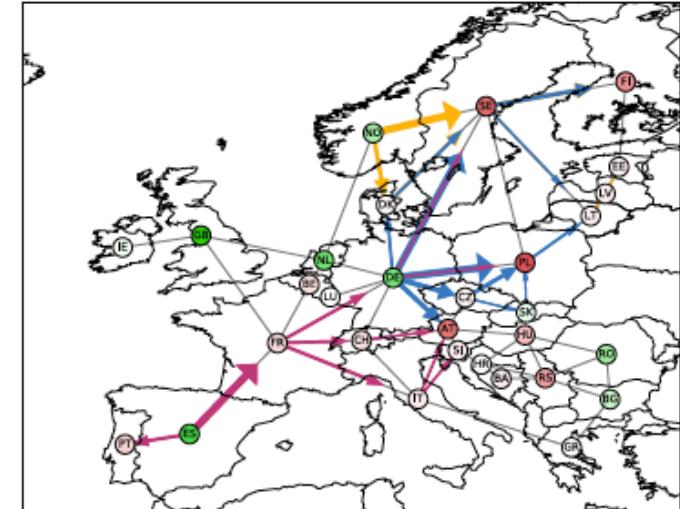
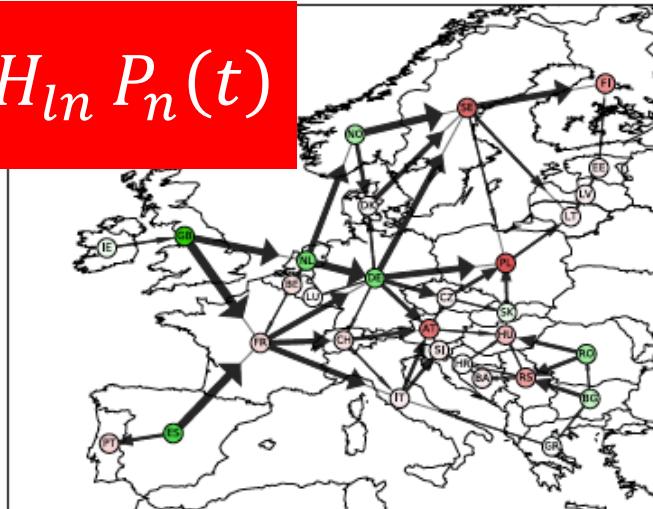
Decompositions of injection patterns for nodal flow allocation in renewable electricity networks

Mirko Schäfer^{1,a}, Bo Tranberg^{1,2}, Sabrina Hempel^{3,b}, Stefan Schramm³, and Martin Greiner¹

THE EUROPEAN
PHYSICAL JOURNAL B

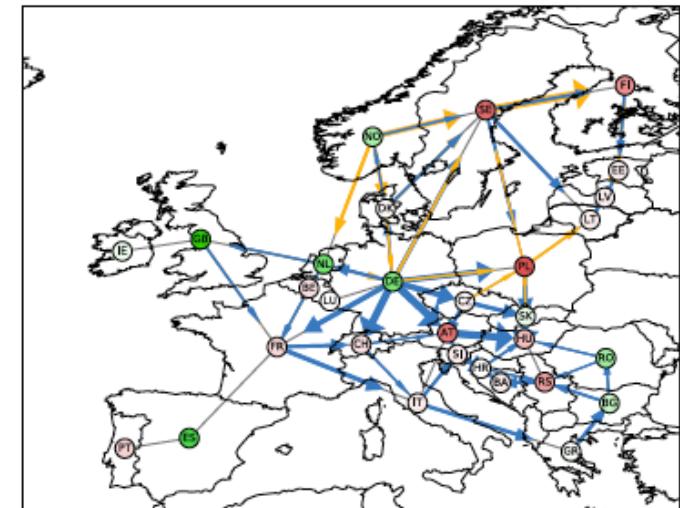
Eur. Phys. J. B (2017) 90: 144
DOI: 10.1140/epjb/e2017-80200-y

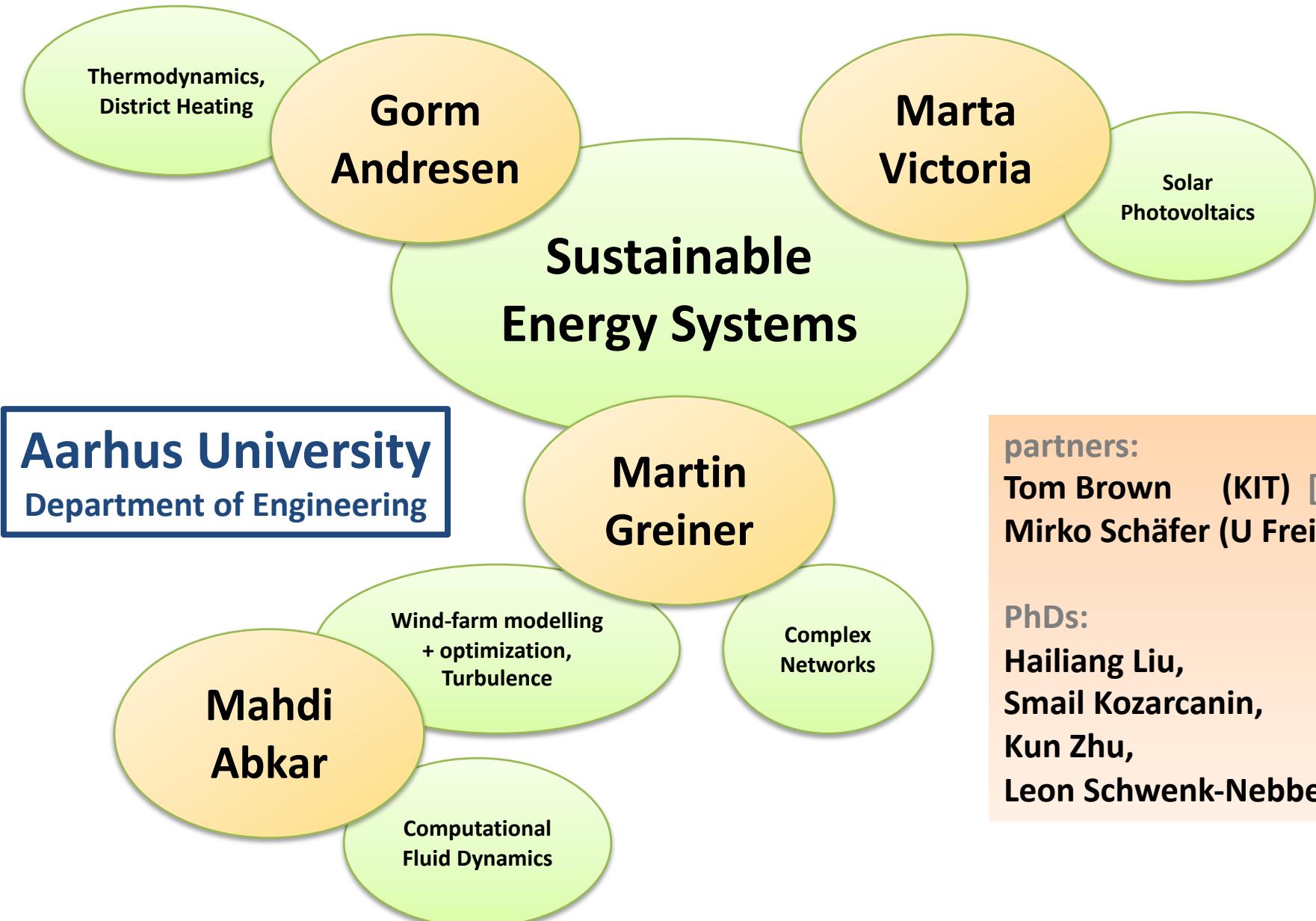
$$F_l(t) = \sum_n H_{ln} P_n(t)$$



$$F_l^{(\alpha)}(t) = \sum_n H_{ln} P_n^{(\alpha)}(t)$$

$$\sum_n P_n^{(\alpha)}(t) = 0 \quad \sum_\alpha P_n^{(\alpha)}(t) = P_n(t)$$

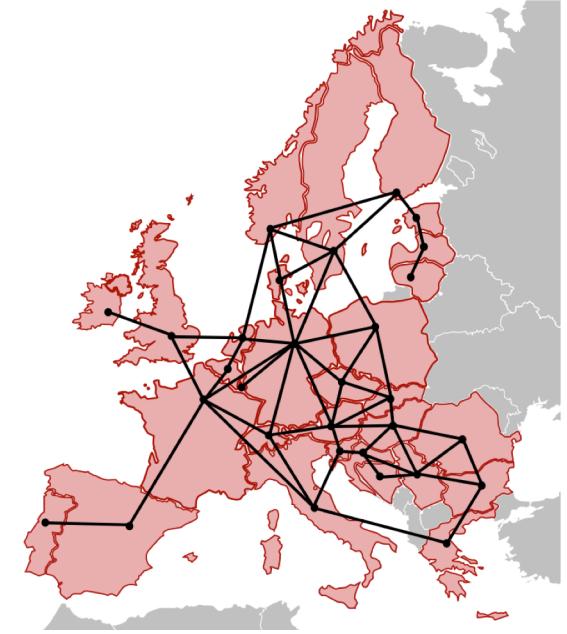
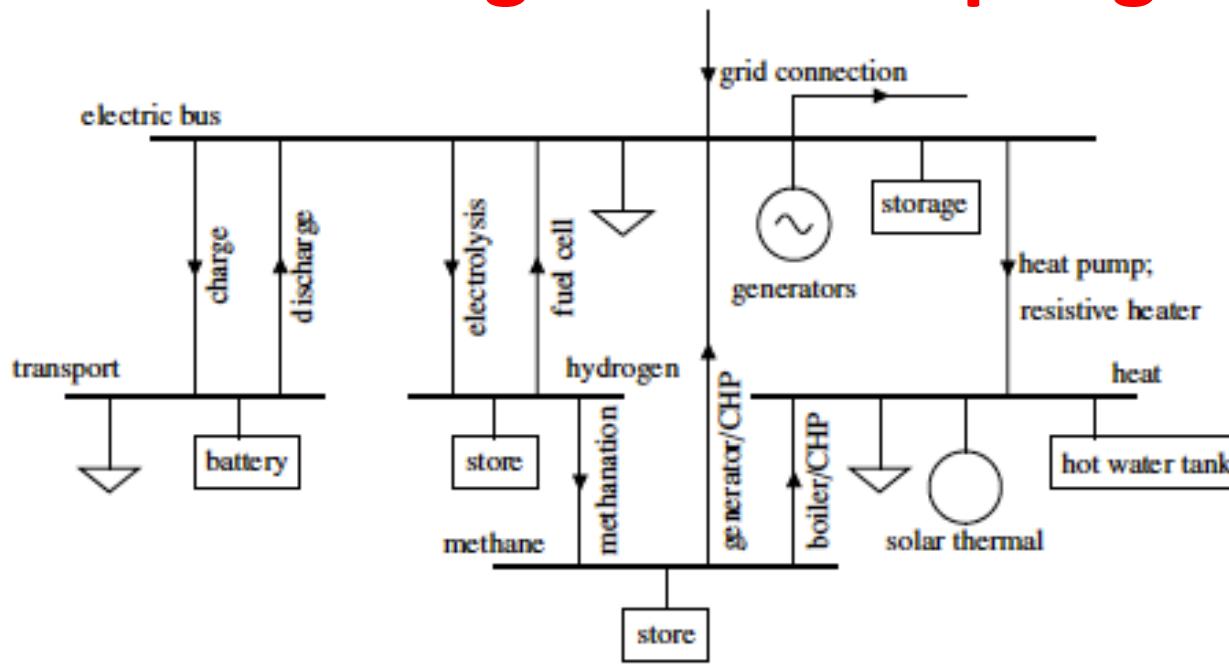




greiner@eng.au.dk

II. Advanced Modeling: electricity → “smart” energy network

Decarbonization of the European energy system with strong sector couplings



- T Brown et.al.,
Energy 160 (2018) 720-39
- K Zhu, M Victoria et.al.,
Applied Energy 236 (2019) 622-34
- T Brown et.al.,
Energies 12 (2019) 1032